

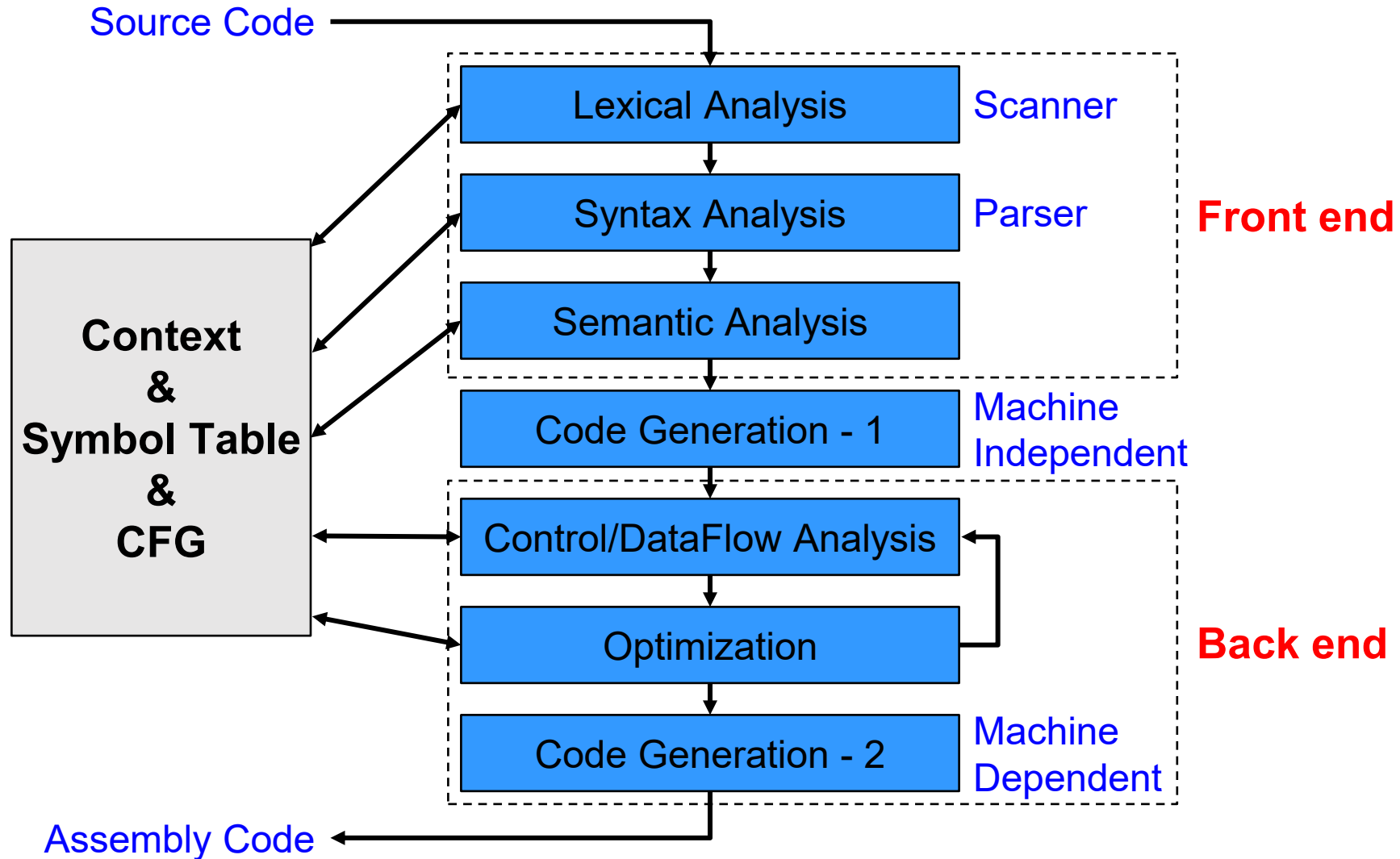
4. Syntax Analysis - 2

2025 Fall

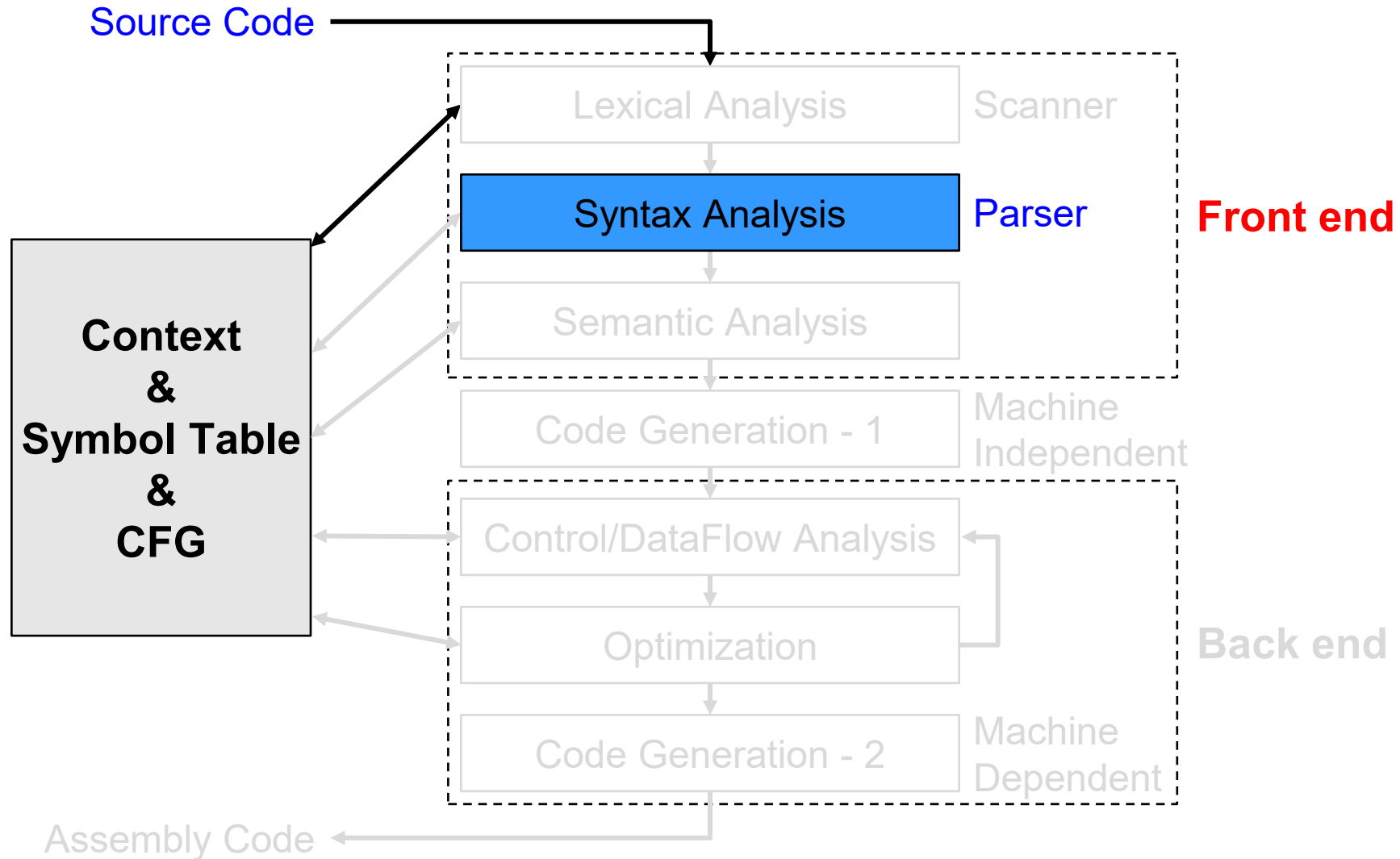
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Syntax Analysis



Syntax Analysis



Specification, Recognition, and Automation in Parser

- **Specification: how to specify valid strings of tokens?**
 - Context-free grammars (CFG)
- **Recognition: how to recognize the specified patterns?**
 - Parse tree and abstract syntax tree (AST)
- **Automation: how to generate parse tree from CFG?**
 - Top-down and bottom-up parsing
 - Automatic generation tool (bison)

Review: Context-Free Grammars (CFG)

- **Terminals are the tokens: keywords, symbols, ID, NUM ...**
- **Non-terminals**
 - program
 - var / expression (arithmetic, logical operations)
 - return / iteration / if statement
- **Start Symbol (S): “program” in compiler**
- **Productions**
 - type-specifier → int | float | bool ...
 - var-declaration → type-specifier ID ; | type-specifier ID [NUM] ;
 - function-declaration → type-specifier ID (params) compound-stmt

Review: More Specifically ...

➔ To Be Covered in the Project

1. *program* → *declaration-list*
2. *declaration-list* → *declaration-list declaration* | *declaration*
3. *declaration* → *var-declaration* | *fun-declaration*
4. *var-declaration* → *type-specifier ID ;* | *type-specifier ID [NUM] ;*
5. *type-specifier* → **int** | **void**
6. *fun-declaration* → *type-specifier ID (params) compound-stmt*
7. *params* → *param-list* | **void**
8. *param-list* → *param-list , param* | *param*
9. *param* → *type-specifier ID* | *type-specifier ID []*
10. *compound-stmt* → { *local-declarations statement-list* }
11. *local-declarations* → *local-declarations var-declarations* | *empty*
12. *statement-list* → *statement-list statement* | *empty*
13. *statement* → *expression-stmt* | *compound-stmt* | *selection-stmt* | *iteration-stmt* | *return-stmt*
14. *expression-stmt* → *expression ;* | *;*

Review: More Specifically ...

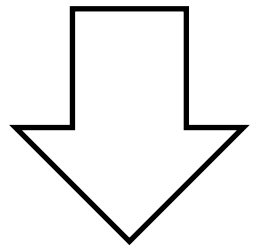
➔ To Be Covered in the Project

- 15. *selection-stmt* $\rightarrow$ **if** (*expression*) *statement* | **if** (*expression*) *statement* **else** *statement*
- 16. *iteration-stmt* $\rightarrow$ **while** (*expression*) *statement*
- 17. *return-stmt* $\rightarrow$ **return** ; | **return** *expression* ;
- 18. *expression* $\rightarrow$ *var* = *expression* | *simple-expression*
- 19. *var* $\rightarrow$ **ID** | **ID** [*expression*]
- 20. *simple-expression* $\rightarrow$ *additive-expression* *relop* *additive-expression* | *additive-expression*
- 21. *relop* $\rightarrow$ <= | < | > | >= | == | !=
- 22. *additive-expression* $\rightarrow$ *additive-expression* *addop* *term* | *term*
- 23. *addop* $\rightarrow$ + | -
- 24. *term* $\rightarrow$ *term* *mulop* *factor* | *factor*
- 25. *mulop* $\rightarrow$ * | /
- 26. *factor* $\rightarrow$ (*expression*) | *var* | *call* | **NUM**
- 27. *call* $\rightarrow$ **ID** (*args*)
- 28. *args* $\rightarrow$ *arg-list* | *empty*
- 29. *arg-list* $\rightarrow$ *arg-list* , *expression* | *expression*

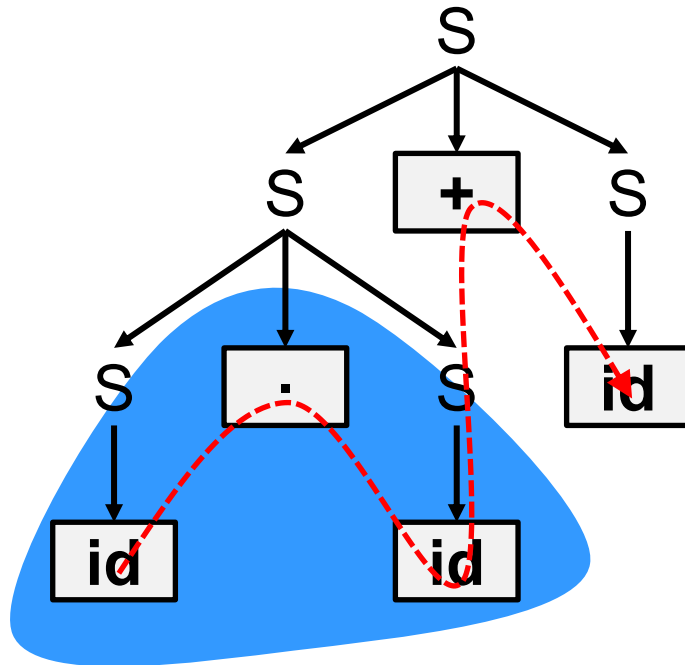
Specification, Recognition, and Automation in Parser

- **Specification:** how to specify valid sequence of tokens?
 - Context-free grammars (CFG)
- **Recognition:** how to recognize the specified patterns?
 - Parse tree and abstract syntax tree (AST)
- **Automation:** how to generate parse tree from CFG?
 - Top-down and bottom-up parsing

Input = id · id + id



$S \rightarrow S + S$
 $\quad | S \cdot S$
 $\quad | id$



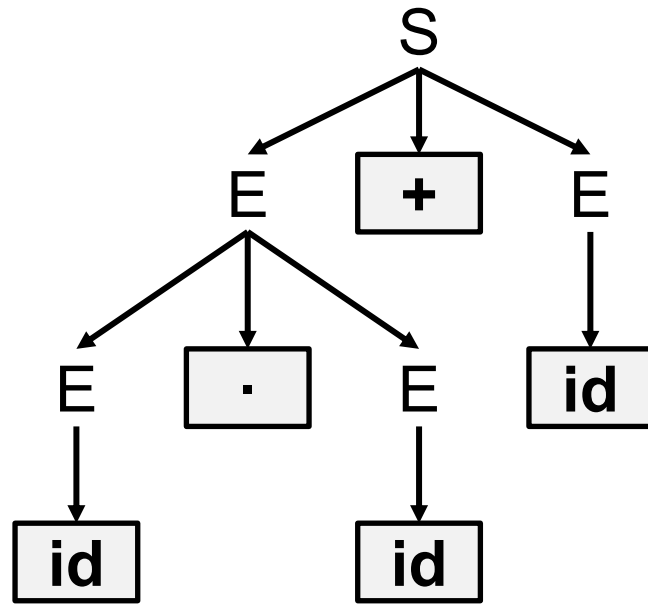
Binds more tightly ($\cdot > +$)

Review: Parse Tree

- **Tree representation of the derivation**
- **A parse tree has**
 - Terminals at the leaves
 - Non-terminals at the interior nodes
- **An in-order traversal of the leaves is the original input**
- **Shows the order of operations**
 - Ex) Operation order, association ...

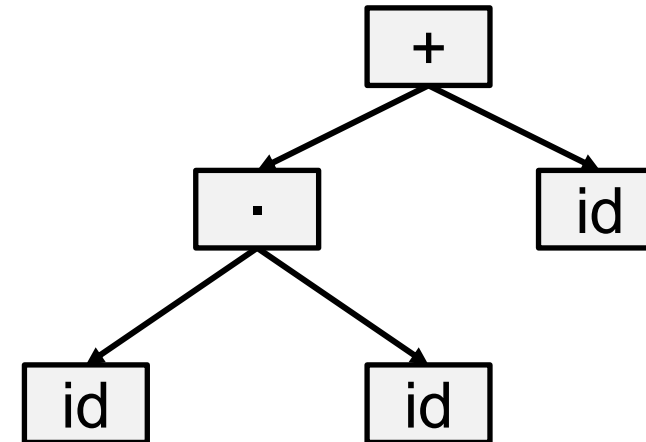
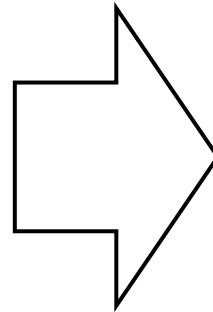
Review: Abstract Syntax Tree (AST)

- AST discards unneeded information for syntax analysis
(Removes non-terminals)



Parse Tree

Remove
details



Abstract Syntax Tree

Specification, Recognition, and Automation in Parser

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- **Automation: how to generate parse tree from CFG?**
 - **Top-down** and bottom-up parsing
 - Automatic generation tool (bison)

Review: Top-Down Parsing

- Construct a leftmost derivation of string while reading the token stream

$S \rightarrow E + S \mid E$
$E \rightarrow \text{num} \mid (S)$

CFG

Partly-derived String

$\rightarrow E + S$
 $\rightarrow (S) + S$
 $\rightarrow (E+S)+S$
 $\rightarrow (1+S)+S$
 $\rightarrow (1+E+S)+S$
 $\rightarrow (1+2+S)+S$
 $\rightarrow (1+2+E)+S$
 $\rightarrow (1+2+(S))+S$
 $\rightarrow \dots$

parsed part **unparsed part**

$(1+2+(3+4))+5$
 $(1+2+(3+4))+5$
 $(1+2+(3+4))+5$
 $(1+2+(3+4))+5$
 $(1+2+(3+4))+5$
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 $(1+2+(3+4))+5$

Derivation Order

Review: Making a Grammar LL(1)

- **LL(1) eliminates the multiple matches in top-down parsing**
 - Left-to-right scanning, Leftmost derivation, and 1 look-ahead symbol
 - We have to read one token to determine which production to apply
- **Left factoring: factor common prefix and add a non-terminal S'**
 - $S \rightarrow E + S \mid E$ is converted as follows
 - $S \rightarrow ES'$ and $S' \rightarrow +S \mid \epsilon$
- **Convert left recursion to right recursion**
 - Example left recursion: $S \rightarrow Sa$ (infinite derivation)
 - We use the term $S \rightarrow^* Sa$ (for some a) to indicate the left recursion

Specification, Recognition, and Automation in Parser

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 - Top-down and **bottom-up parsing**
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Bottom-Up Parsing - 1

- **Bottom-up parsing is more efficient than Top-down parsing using LR grammars**
 - Construct right-most derivation of program
 - Left-recursive grammars, and Right-most derivation
- **Rely on shift-reduce parsers**
 - The parser either shifts to the next input token or reduce the symbols (we'll get to this later on)

Bottom-Up Parsing - 2

- **Right-most derivation** requires reducing symbols to the start symbol by “inverting” productions
 - Match RHS of production and replace it by LHS

CFG

$E \rightarrow T \mid T + E$
$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

Bottom-Up Parser

Reduce

Input string	Applied production
int * int + int	$T \rightarrow \text{int}$
int * T + int	$T \rightarrow \text{int} * T$
T + int	$T \rightarrow \text{int}$
T + T	$E \rightarrow T$
T + E	$E \rightarrow T + E$
E	

Right-most derivation

Shift-Reduce Parsing

- **Bottom-up parser traces a rightmost derivation in reverse**
 - We should scan the input terminals in a left-to-right manner
- **We can split a string into two parts: sequence of symbols to reduce (stack) + remaining tokens (input)**
- **Shift reduce parsing requires two actions**
 - Reduce using symbols in the stack (**Reduce**)
 - Scan the left-most token in the input and move it to the stack (**Shift**)

Shift-Reduce Parsing Example

CFG

$E \rightarrow T \mid T + E$ $T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

Shift-Reduce Parser

Stack	Input string	Applied production
	int * int + int	shift
int	* int + int	shift
int *	int + int	shift
int * int	+ int	reduce $T \rightarrow \text{int}$
int * T	+ int	reduce $T \rightarrow \text{int} * T$
T	+ int	shift
T +	int	shift
T + int		reduce $T \rightarrow \text{int}$
T + T		reduce $E \rightarrow T$
T + E		reduce $E \rightarrow T + E$
E		

Key Challenge: Action Selection Problem

- **Which action should we take?**
 - Should we shift?
 - Should we reduce? If so, which production should we applied?
- **There are conflicts**
 - For a given state (stack + input), there can be multiple possible actions
 - Shift-reduce conflict: can both shift and reduce
 - Reduce-reduce conflict: can apply two different productions

$E \rightarrow T \mid T + E$ $T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

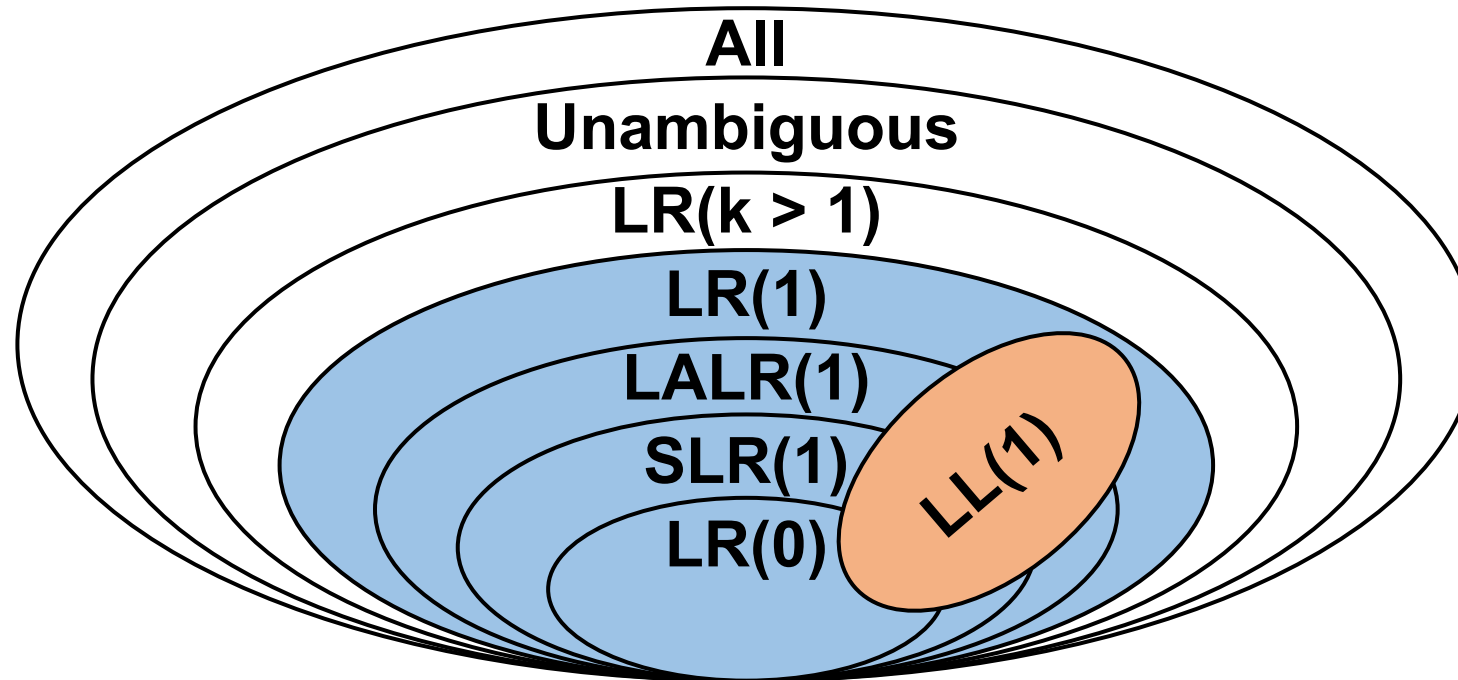
Stack	Input String
int	* int + int

Lookahead?

**Shift vs.
Reduce**

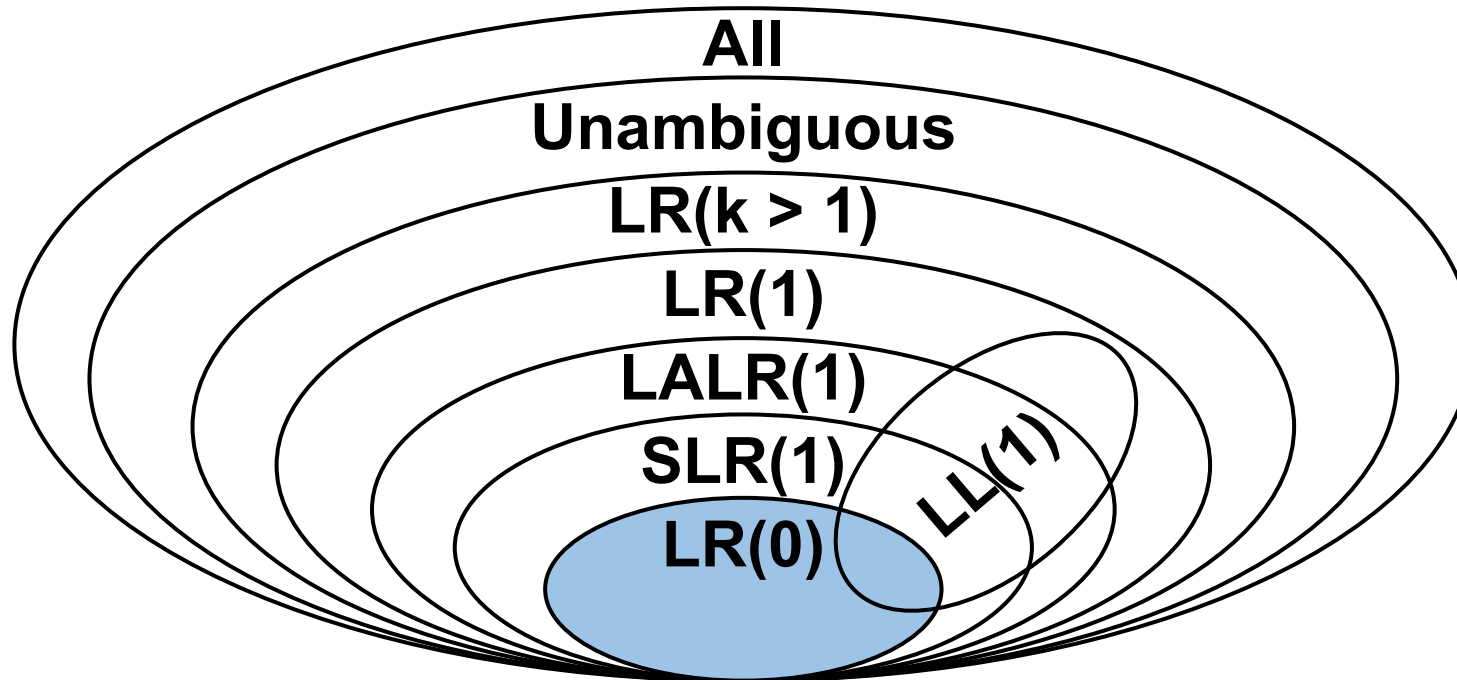
LR-Style Grammars

- LR(k): left-to-right scanning, right-most derivation, and k symbol lookahead
- There are variations of the LR(k) (i.e., LALR, SLR)



LR(0) Grammars

- **LR(0)** indicates grammars that can determine actions w/o any lookahead
 - There are no reduce-reduce and shift-reduce conflicts when using only the symbols in the stack



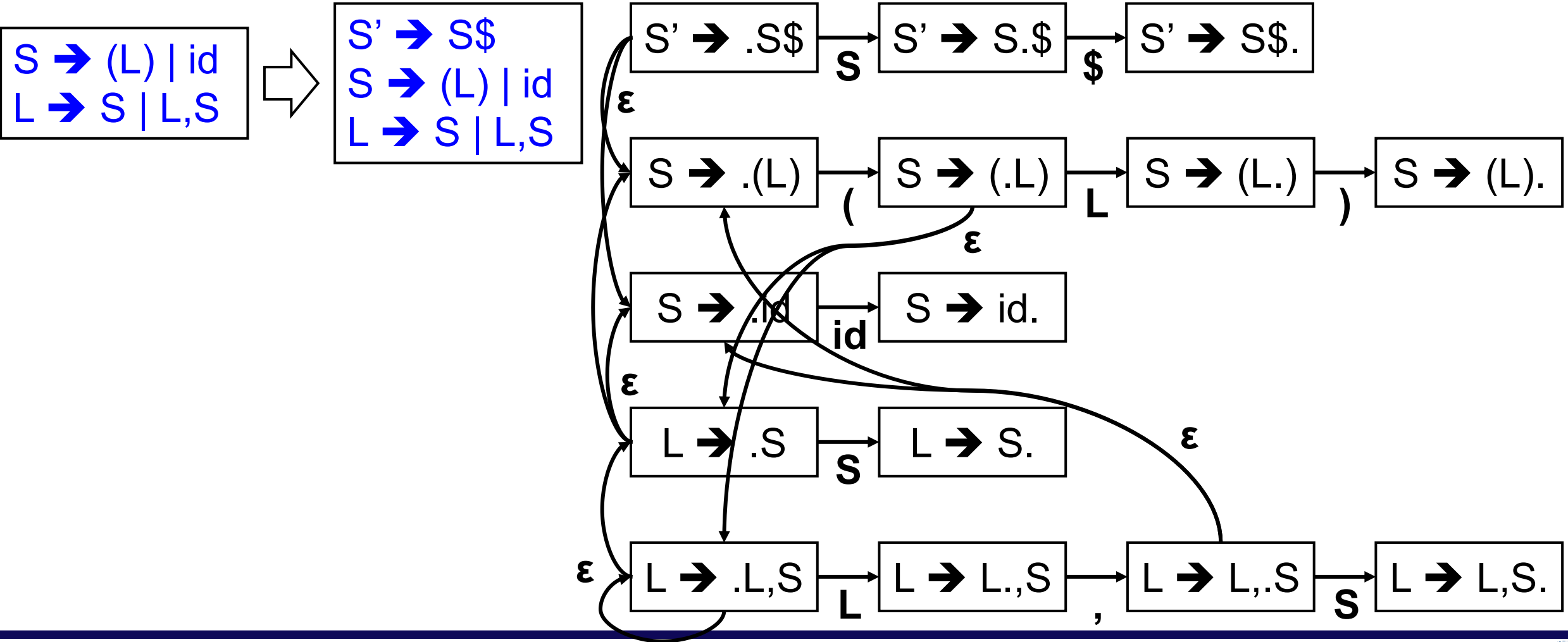
NFA Representation

- **We can represent shift-reduce parsing using an NFA**
 - The states are items, which are productions with a separator “.” on RHS
 - Ex) $T \rightarrow (E)$ has four items: $T \rightarrow \cdot(E)$, $T \rightarrow (\cdot E)$, $T \rightarrow (E\cdot)$, and $T \rightarrow (E)\cdot$.
 - $T \rightarrow (\cdot E)$ indicates that “(” is on the stack and we expect to see “E” in the upcoming input
 - We have an additional dummy production $S' \rightarrow S\$$ for a start and end state
- **There are two types of transitions between the states**
 - Shift transition: transition by the shift actions
 - There is a transition between State: $\{T \rightarrow (\cdot E)\}$ and State: $\{T \rightarrow (E\cdot)\}$ if the left most symbol of the input string is “E”
 - ϵ -transition: we see another production that stems from the expected symbol
 - State: $\{T \rightarrow (\cdot E)\}$ becomes State: $\{E \rightarrow \cdot T\}$ and State: $\{T \rightarrow \cdot T + E\}$

LR(0) NFA Representation Example

LR(0) CFG

NFA



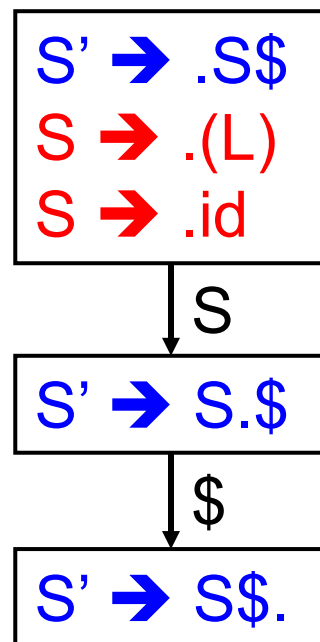
LR(0) DFA Representation

- Recall NFA to DFA: Group NFA states with ϵ -closure (closure)!
 - For Closure(s) which keeps $\{A \rightarrow \alpha.B\beta\}$, and $\{B \rightarrow \gamma\}$ is a production, add $\{B \rightarrow \gamma.\}$ to the production

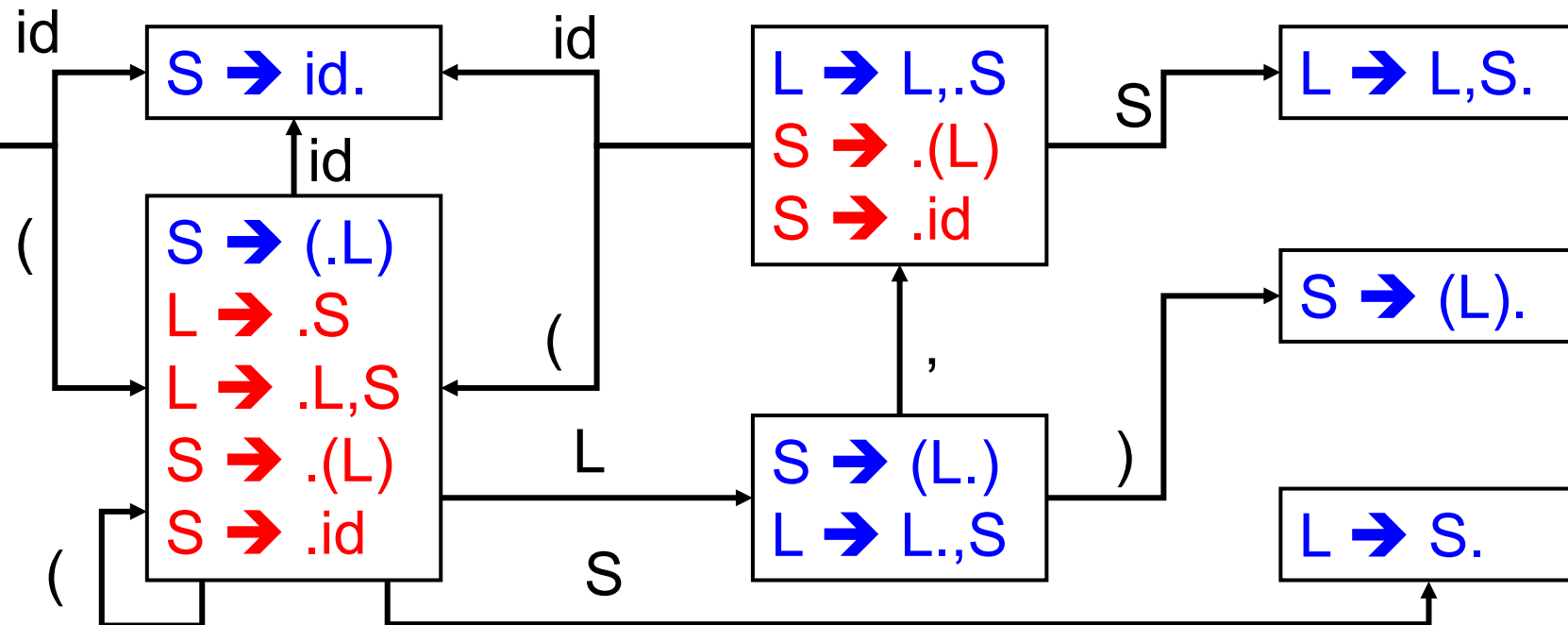
LR(0) CFG

$S' \rightarrow S$
 $S \rightarrow (L) \mid id$
 $L \rightarrow S \mid L,S$

Closure

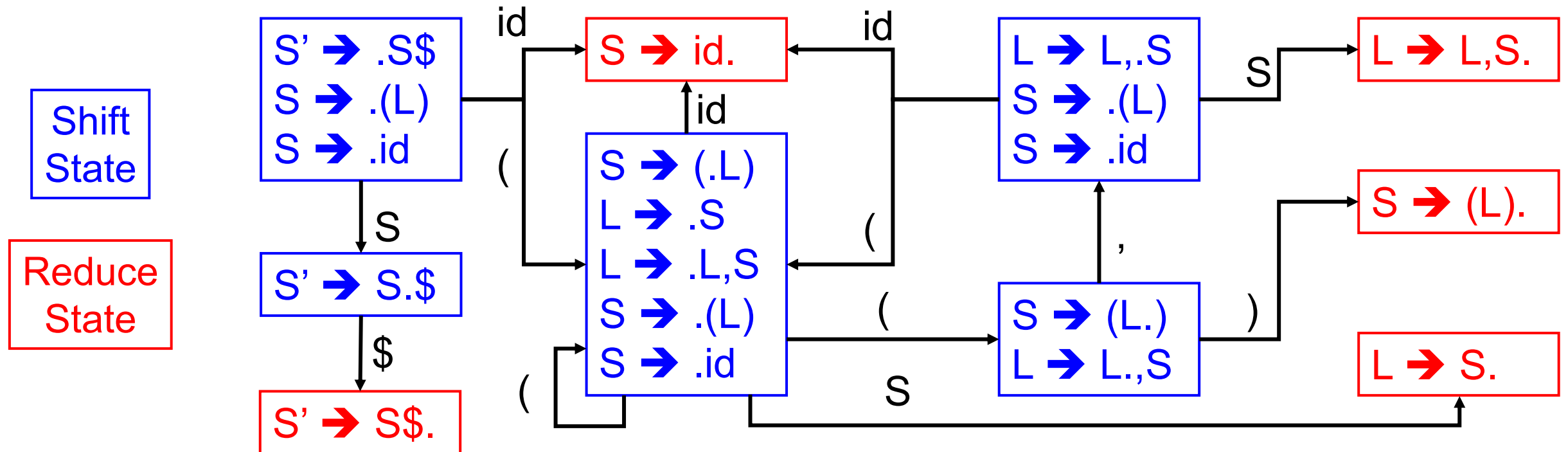


DFA



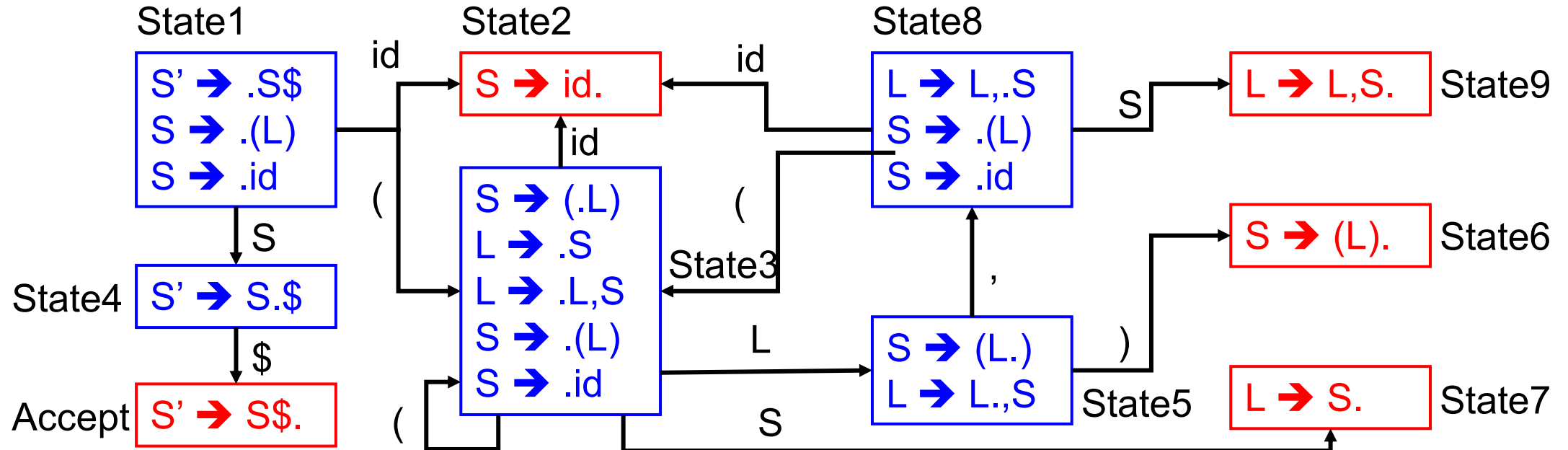
LR(0) Parsing Using DFA

- Using the DFA, we determine whether to shift or reduce
 - We use symbols in the stack to traverse the state
 - Use the destination state to determine whether to shift or reduce



LR(0) Parsing Using DFA Example

stack	input	action
(	((a),b)	
((	(a),b)	
((a	a),b)	
((a	),b)	
((S	),b)	

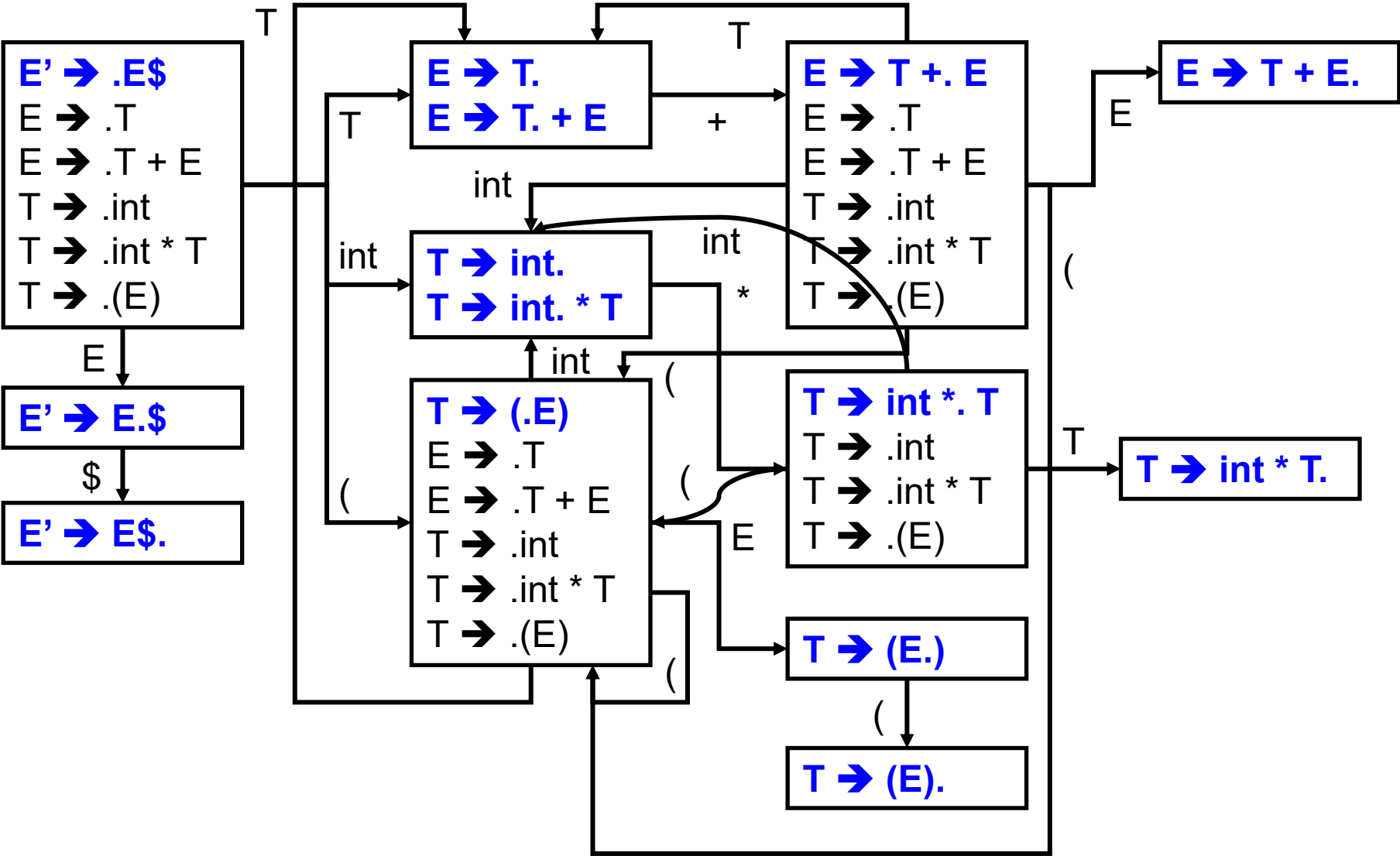


Class Exercise

- **Generate the DFA for the following grammar**
 - You will need a large space!

$E \rightarrow T \mid T + E$
$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

$E \rightarrow T \mid T + E$
 $T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

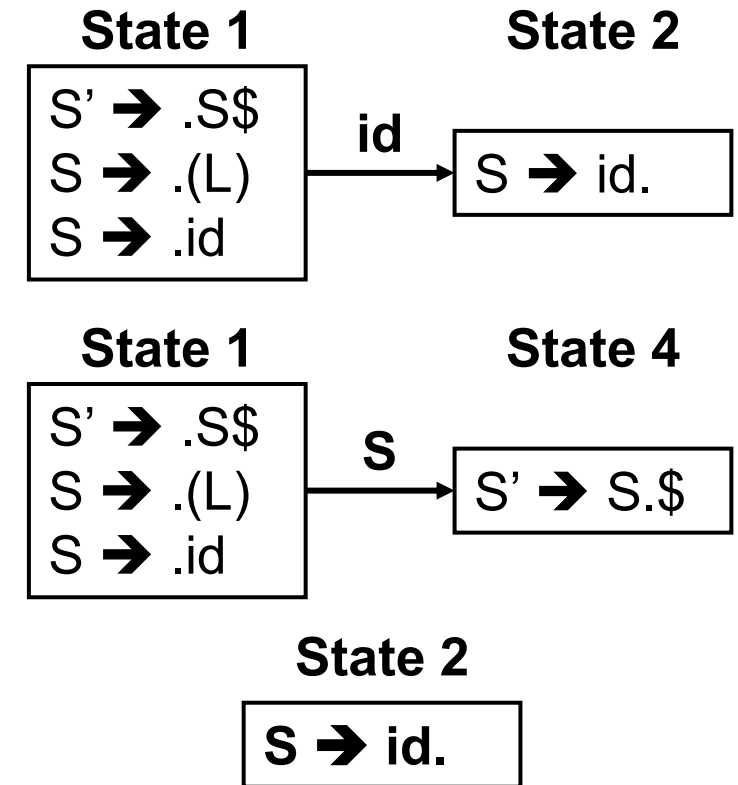


DFA Traversal Implementation

- **Store “the states along with the symbols” in the stack**
 - $\langle \text{symbol}, \text{state} \rangle$ and start using the top $\langle \text{symbol}, \text{state} \rangle$ on the stack
- **There are two different types of tables**
 - goto: determine the next state using the top state and an input non-terminal
 - action: determine the action using the top state and an input terminal
- **There are four different actions**
 - Shift x : push $\langle a, x \rangle$ on the stack (a is the current input and x is a state)
 - Reduce $x \rightarrow \alpha$: pop α from the stack and push $\langle x, \text{goto}[\text{curr_state}, x] \rangle$
 - Accept ($S' \rightarrow S\$$) / Error (no valid action available)

LR Parsing Table Generation

- We can simplify the DFA using a parsing table
- DFA states are converted to index of each rows
- For transition $S_{old} \rightarrow S_{new}$ on terminal C:
 - $Table[S_{old}, C] += Shift(S_{new})$
- For transition $S_{old} \rightarrow S_{new}$ on non-terminal N:
 - $Table[S_{old}, N] += Goto(S_{new})$
- If S is a reduction state $X \rightarrow \beta$ then:
 - $Table[S, *] += Reduce(X \rightarrow \beta)$



LR Parsing Table

- We can simplify the DFA using a parsing table

	(	)	id	,	\$	S	L
State 1	Shift 3		Shift 2			Goto 4	
State 2	S → id						
State 3	Shift 3		Shift 2			Goto 7	Goto 5
State 4					Accept		
State 5		Shift 6		Shift 8			
State 6	S → (L)						
State 7	L → S						
State 8	Shift 3		Shift 2			Goto 9	
State 9	L → L,S						

Action Table

Goto Table

Recall: Action Selection Problem

- **Which action should we take?**
 - Should we shift?
 - Should we reduce? If so, which production should we applied?
- **There are conflicts**
 - For a given state (stack + input), there can be multiple possible actions
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$E \rightarrow T \mid T + E$ $T \rightarrow \text{int} \mid \text{int} * T \mid (E)$

Stack	Input String
int	* int + int

Lookahead?

**Shift vs.
Reduce**

Parsing Implementation

```
// I is an input stream
// j = 0
// DFA state 1 is the start state
stack = <dummy, 1>
repeat
    case action[top_state(stack), I[j]]
        shift X: push <I[j++], X>
        reduce X → A:
            pop |A| pairs
            push <X, goto[top_state(stack), X]>
        accept: halt normally
        error: halt and report error
end
```

LR Parsing Table

- We can simplify the DFA using a parsing table

	(	)	id	,	\$	S	L
State 1	Shift 3		Shift 2			Goto 4	
State 2	S → id						
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State 5		Shift 6		Shift 8			
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Action Table

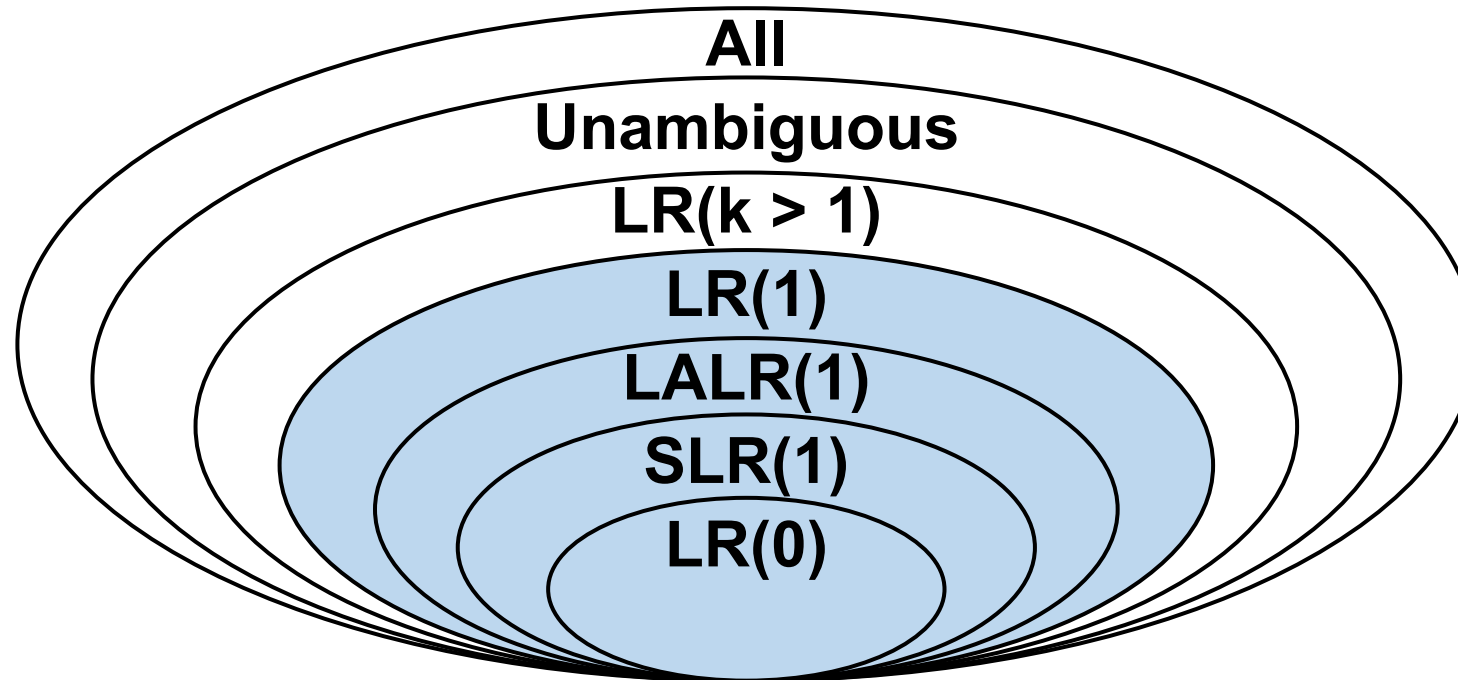
Goto Table

Parsing Using Table Example

stack	input	action
<dummy, 1>	((a),b)\$	
<dummy, 1><(, 3>	(a),b)\$	
<dummy, 1><(, 3><(, 3>	a),b)\$	
<dummy, 1><(, 3><(, 3><a, 2>	),b)\$	
<dummy, 1><(, 3><(, 3><S, 7>	),b)\$	
<dummy, 1><(, 3><(, 3><L, 5>	),b)\$	
<dummy, 1><(, 3><(, 3><L, 5><), 6>	,b)\$	
<dummy, 1><(, 3><S, 7>	,b)\$	
<dummy, 1><(, 3><L, 5>	,b)\$	
<dummy, 1><(, 3><L, 5><,, 8>	b)\$	
<dummy, 1><(, 3><L, 5><,, 8><b, 2>	)\$	
<dummy, 1><(, 3><L, 5><,, 8><S, 9>	)\$	
<dummy, 1><(, 3><L, 5>	)\$	
<dummy, 1><(, 3><L, 5><), 6>	\$	
<dummy, 1><S, 4>	\$	

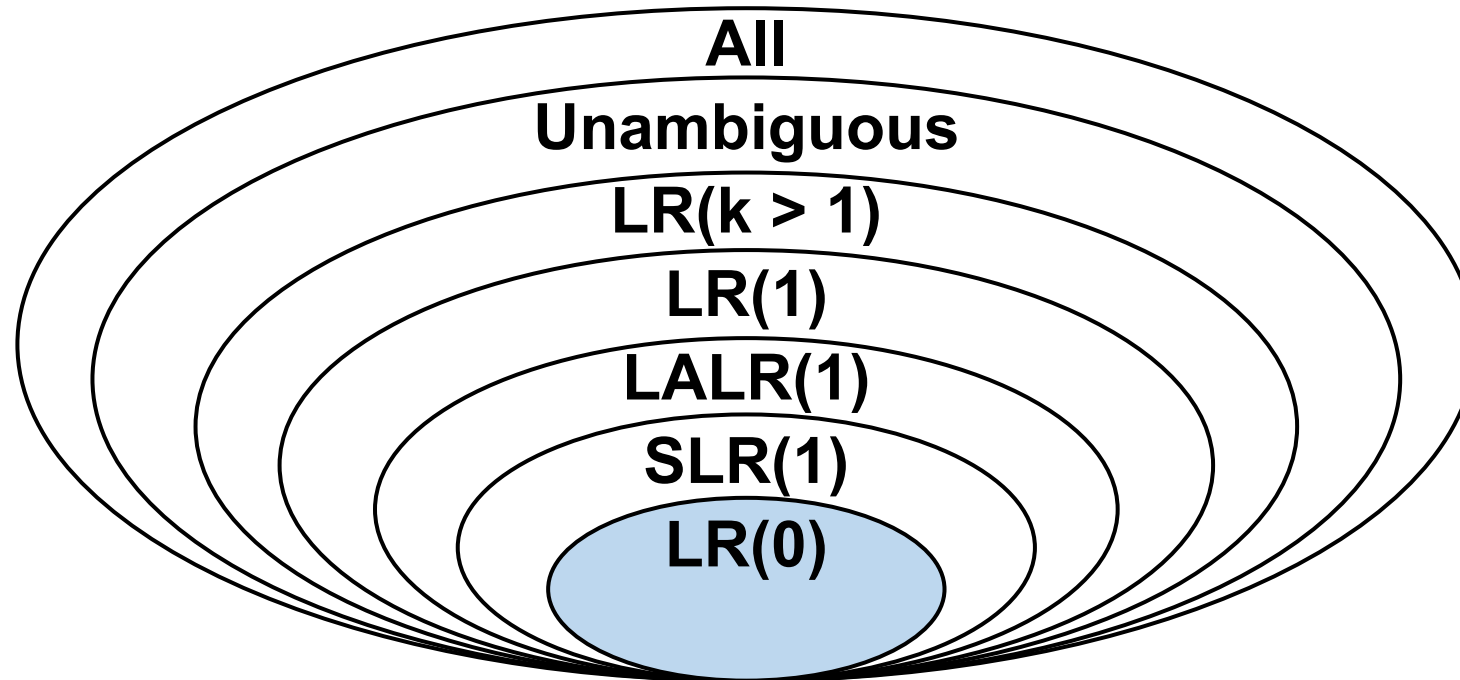
LR-Style Grammars

- **LR(k): left-to-right scanning, right-most derivation, and k lookahead**
- **There are variations of the LR(k) (i.e., LALR, SLR)**



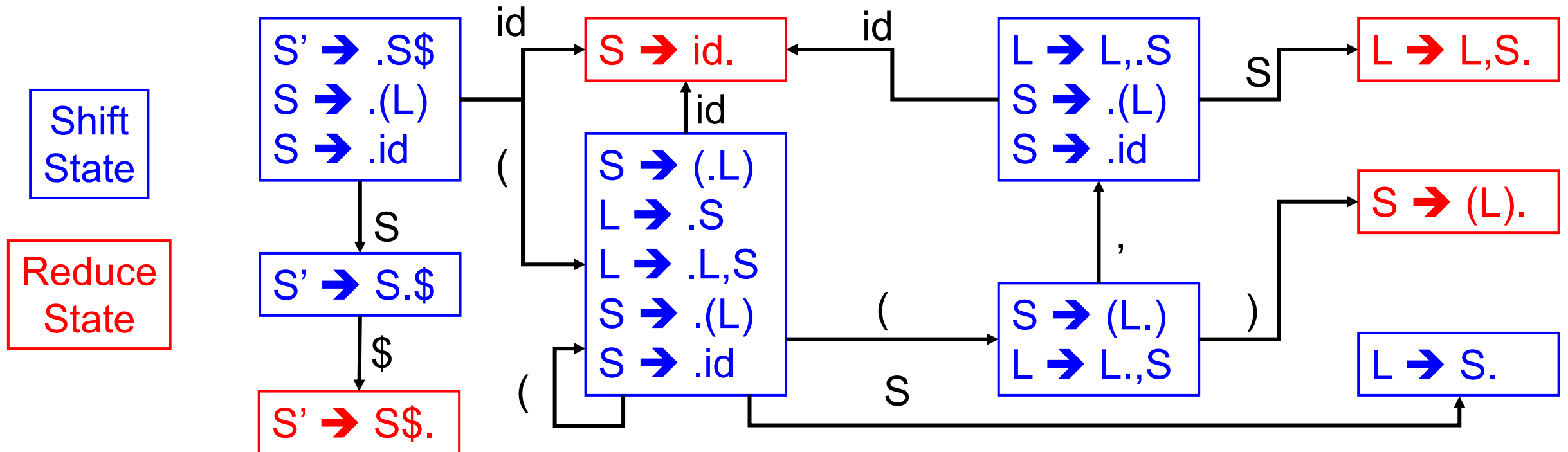
LR(0) Grammars

- LR(0) assumes no shift-reduce and reduce-reduce conflicts even without lookahead



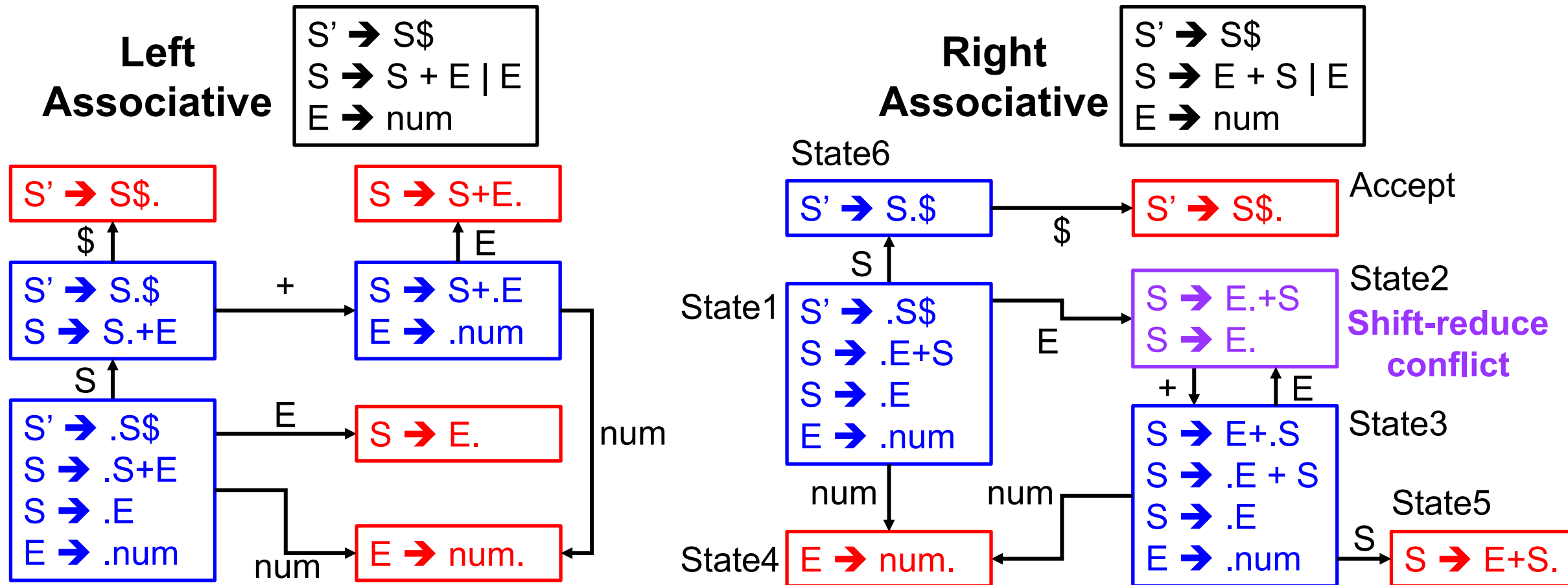
LR(0) Limitations

- An LR(0) parser only works if states with reduce actions have a single reduction action (no other reduction or shift)



A Non-LR(0) Grammar

- Right-associative is not LR(0); there is a shift-reduce conflict!



A Non-LR(0) Grammar

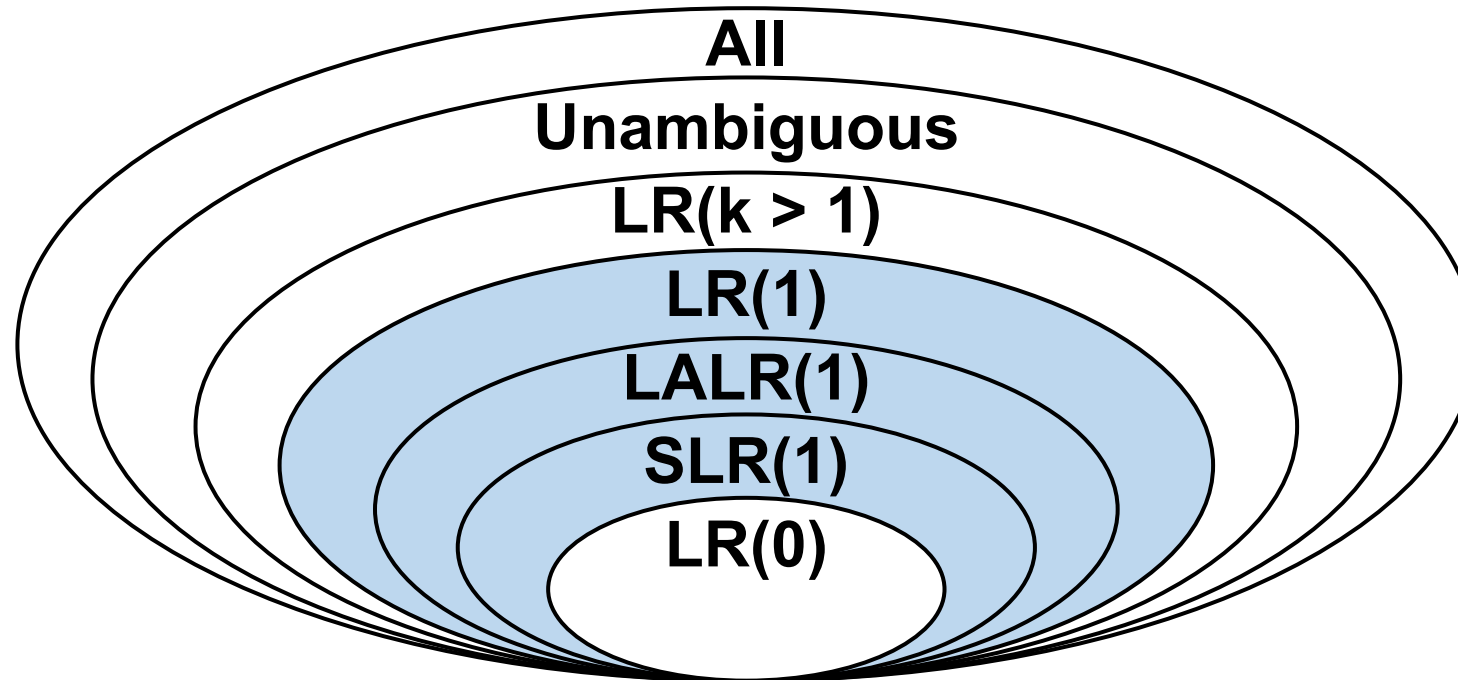
- There are multiple options to fill the parsing table

	num	+	\$	E	S
State 1	Shift 4			Goto 2	Goto 6
State 2	$S \rightarrow E$	$S \rightarrow E$ vs. Shift 3	$S \rightarrow E$		
State 3	Shift 4			Goto 2	Goto 5
State 4	$E \rightarrow \text{num}$	$E \rightarrow \text{num}$	$E \rightarrow \text{num}$		

⋮

Solve Conflict With Lookahead

- There are three popular techniques for employing lookahead of a single symbol
 - Each has a different mean of utilizing the lookahead!



SLR(1) Parsing

- **A simple extension of LR(0)**
 - For each reduction $X \rightarrow \beta$, look at the next symbol γ
 - Apply reduction only if γ is in $\text{Follow}(X)$
 - Ex) $\alpha\beta\gamma$ can become $\alpha X\gamma$ only if γ is in $\text{Follow}(X)$
- **SLR(1) (a.k.a., SLR) parsing table can eliminate conflict**

$S' \rightarrow S\$$
 $S \rightarrow E + S \mid E$
 $E \rightarrow \text{num}$



$\text{Follow}(S) = \{\$, \}$

	num	+	\$	E	S
State 1	Shift 4			Goto 2	Goto 6
State 2	$S \rightarrow E$	$S \rightarrow E$ Shift 3	$S \rightarrow E$		

SLR Parsing Table

- Do not fill the entire rows as before

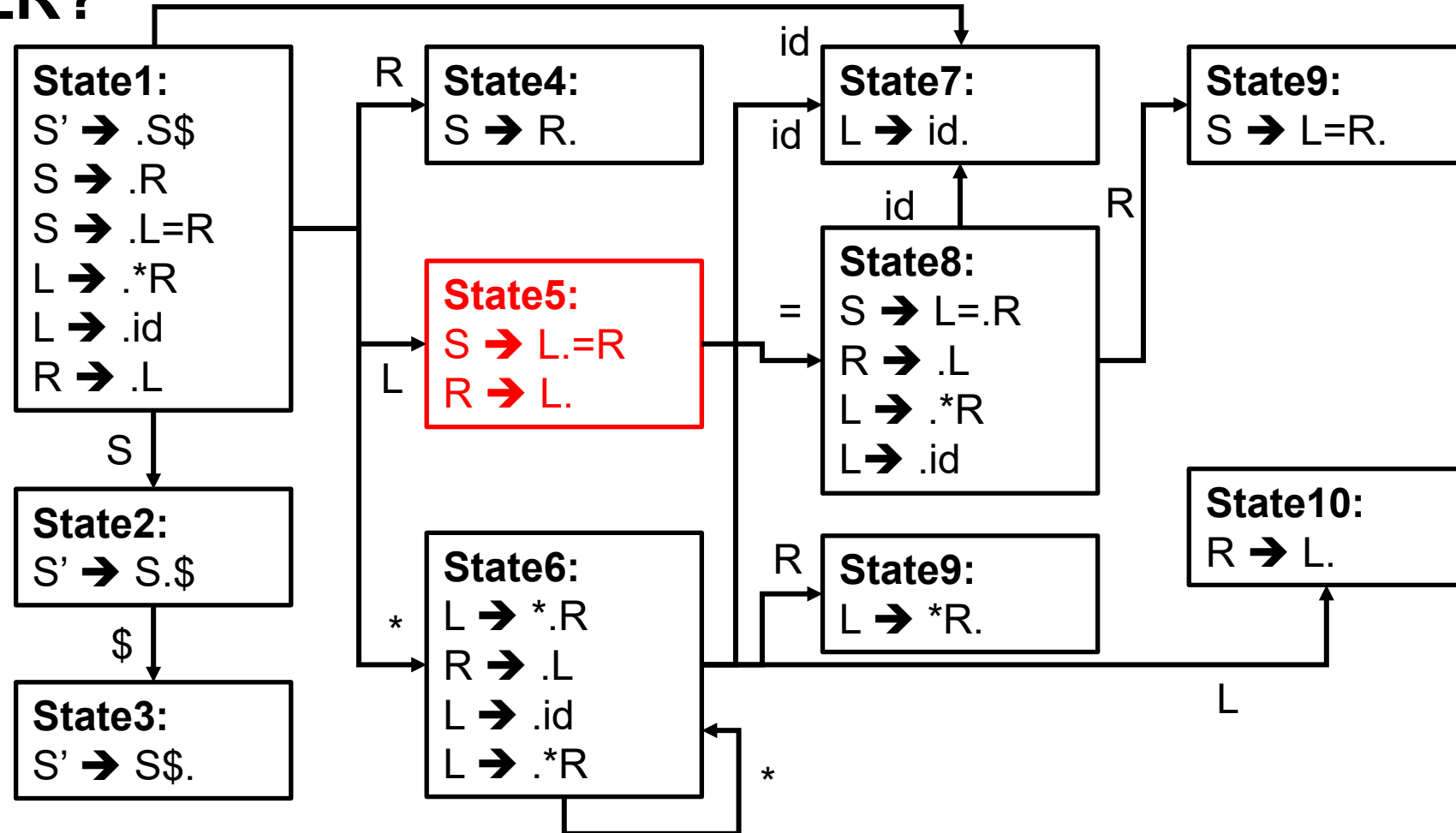
	num	+	\$	E	S
State 1	Shift 4			Goto 2	Goto 6
State 2		Shift 3	$S \rightarrow E$		
State 3	Shift 4			Goto 2	Goto 5
State 4		$E \rightarrow \text{num}$	$E \rightarrow \text{num}$		
State 5			$S \rightarrow E+S$		
State 6			Shift 7		
State 7			accept		

Class Exercise

- Is this grammar SLR?

- $S \rightarrow L = R$
- $S \rightarrow R$
- $L \rightarrow *R$
- $L \rightarrow id$
- $R \rightarrow L$

Hint: Check if $=$ follows R



LR(1) Parsing

- We use more out of the lookahead symbol
- LR(1) determines whether to shift or reduce using a lookahead
- Uses a more complex state $X \rightarrow \alpha.\beta$, γ
 - Meaning: α already matched at top of the stack, next expect to see β , followed by γ
 - $[X \rightarrow \alpha.\beta, \{x_1, x_2, \dots, x_n\}]$ indicates a set of states:
 - $X \rightarrow \alpha.\beta, x_1$
 - ...
 - $X \rightarrow \alpha.\beta, x_n$
- We extend the ϵ -closure and goto operations

LR(1) Closure

- **LR(1) closure identification:**
 - Start with $\text{Closure}(S) = S$
 - For each item in $S [X \rightarrow \alpha . B \beta, \lambda]$
 - Add $\{B \rightarrow .\gamma, \text{First}(\beta\lambda)\}$
- **Initialize the state with $[S' \rightarrow .S, \$]$ and apply closure**

CFG

$S' \rightarrow S\$$
$S \rightarrow E + S \mid E$
$E \rightarrow \text{num}$

Start State

$S' \rightarrow .S$	$\$$
---------------------	------



Closure

$S' \rightarrow .S$	$\$$
$S \rightarrow .E + S$	$\text{First}(\$) \rightarrow \$$
$S \rightarrow .E$	$\text{First}(\$) \rightarrow \$$
$E \rightarrow .\text{num}$	$\text{First}(+S\$) + \text{First}(\$) \rightarrow +, \$$

LR(1) Goto

- **LR(1) goto operations:**

- Given an item in the state I ($X \rightarrow \alpha . B \beta, \lambda$),
- $\text{Goto/Shift}(I, B) = \text{Closure}([X \rightarrow \alpha B . \beta, \lambda])$

CFG

$S' \rightarrow S\$$
$S \rightarrow E + S \mid E$
$E \rightarrow \text{num}$

State I

$S \rightarrow E.+S$	\$
$S \rightarrow E.$	\$

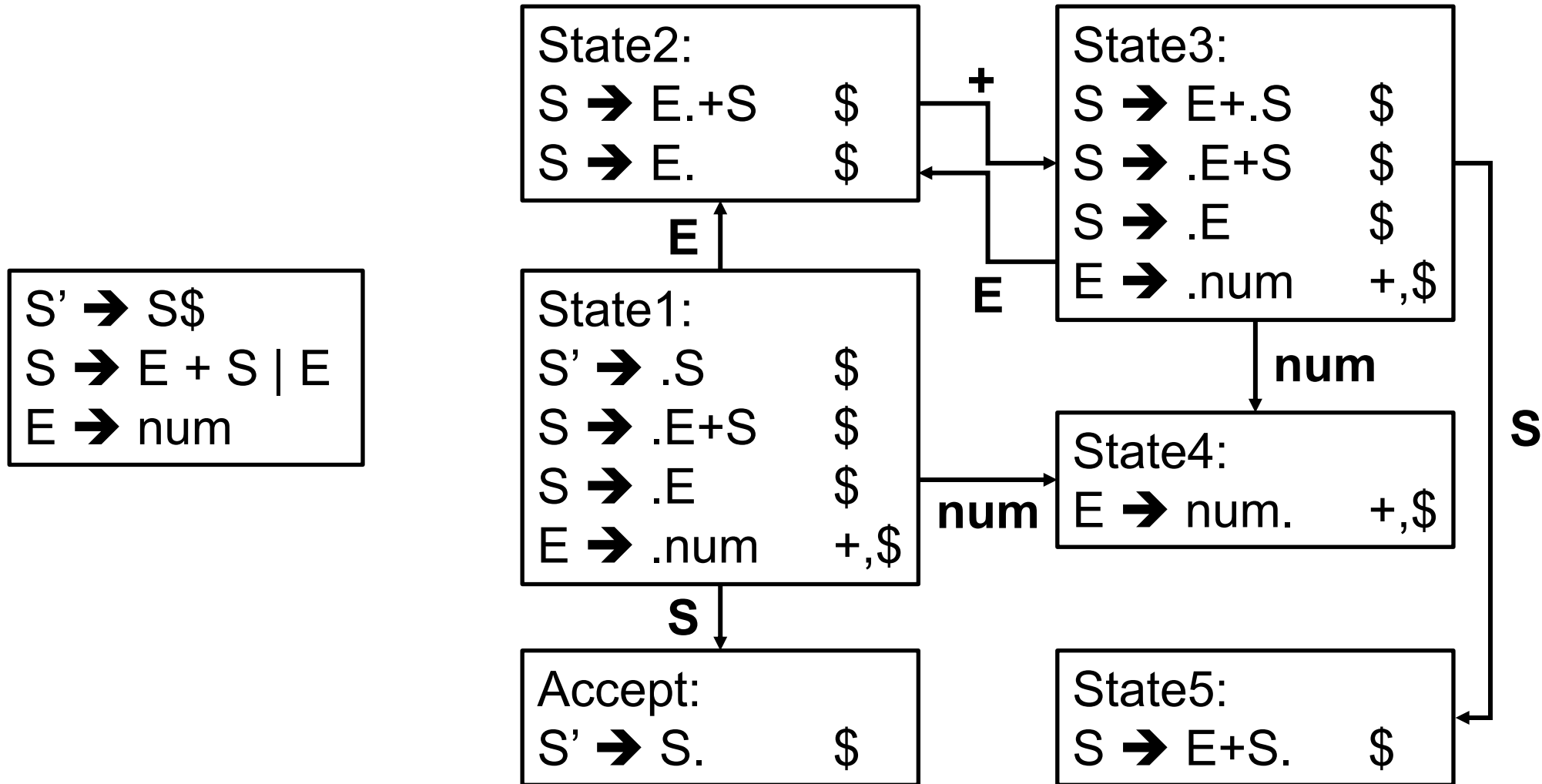


Goto/Shift (I, +)

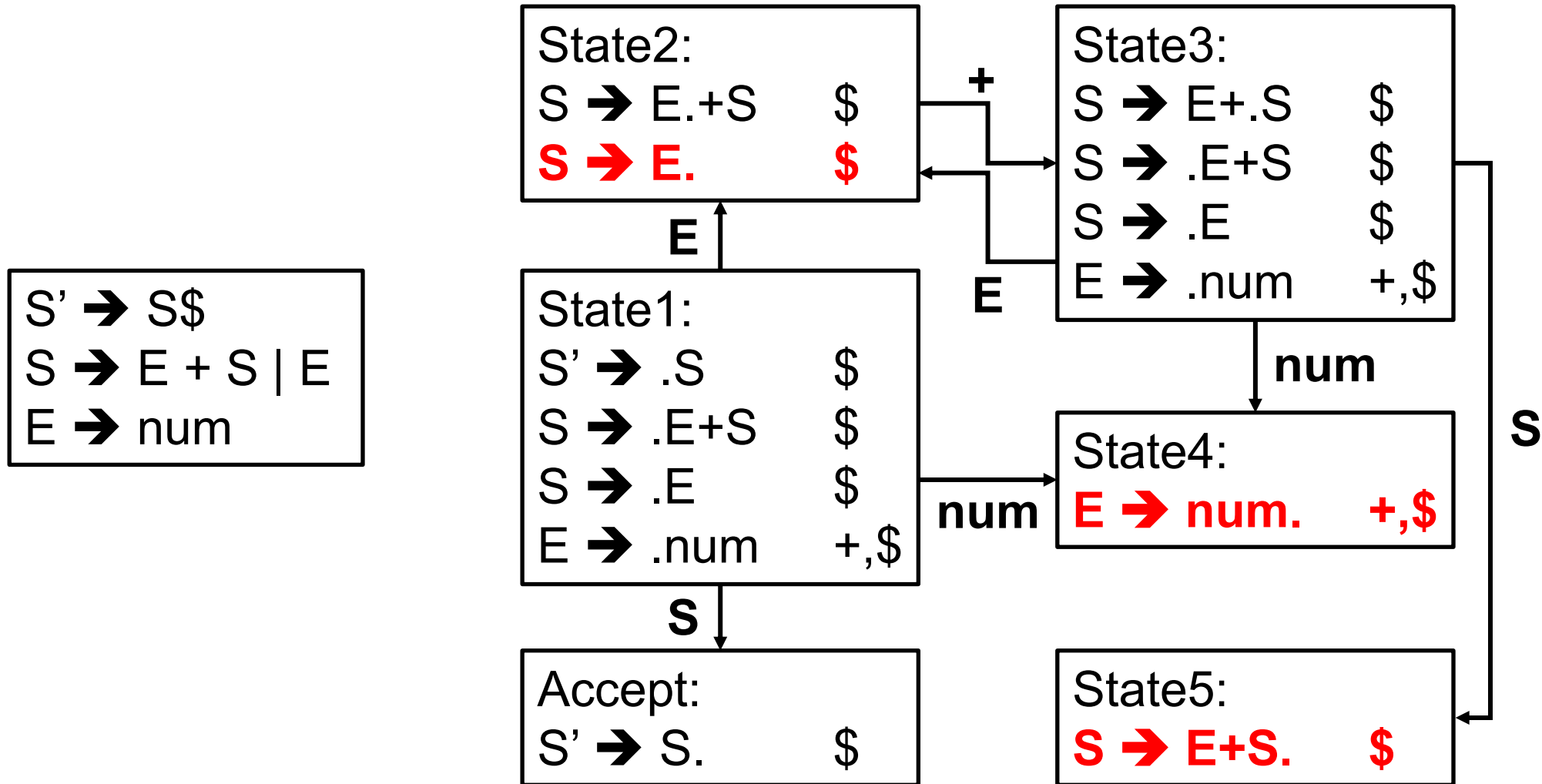
$\text{Closure}([S \rightarrow E + .S,$	\$])
---	------

$S \rightarrow E+.S$	\$
$S \rightarrow .E+S$	\$
$S \rightarrow .E$	\$
$E \rightarrow .\text{num}$	+, \$

LR(1) DFA Example



LR(1) Reduction



LR(1) Parsing Table

- Same as LR(0) parsing table construction, except for reductions

- For a transition $S \rightarrow S'$ on terminal x :

- $\text{Table}[S, x] = \text{Shift}(S')$

- For a transition $S \rightarrow S'$ on non-terminal N :

- $\text{Table}[S, N] = \text{Goto}(S')$

- If I contains $[X \rightarrow \alpha, \beta]$ then:

- $\text{Table}[I, \beta] = \text{Reduce}(X \rightarrow \alpha)$

LR(1)

$S \rightarrow E.+S$	\$
$S \rightarrow E.$	\$

Reduce if
lookahead is \$

SLR

$S \rightarrow E.+S$
$S \rightarrow E.$

Reduce if lookahead
is $\text{Follow}(S) = \{\$ \}$

Class Exercise

- Draw RL(1) DFA for the following grammar
 - $S \rightarrow L = R$
 - $S \rightarrow R$
 - $L \rightarrow *R$
 - $L \rightarrow \text{id}$
 - $R \rightarrow L$

Hint:

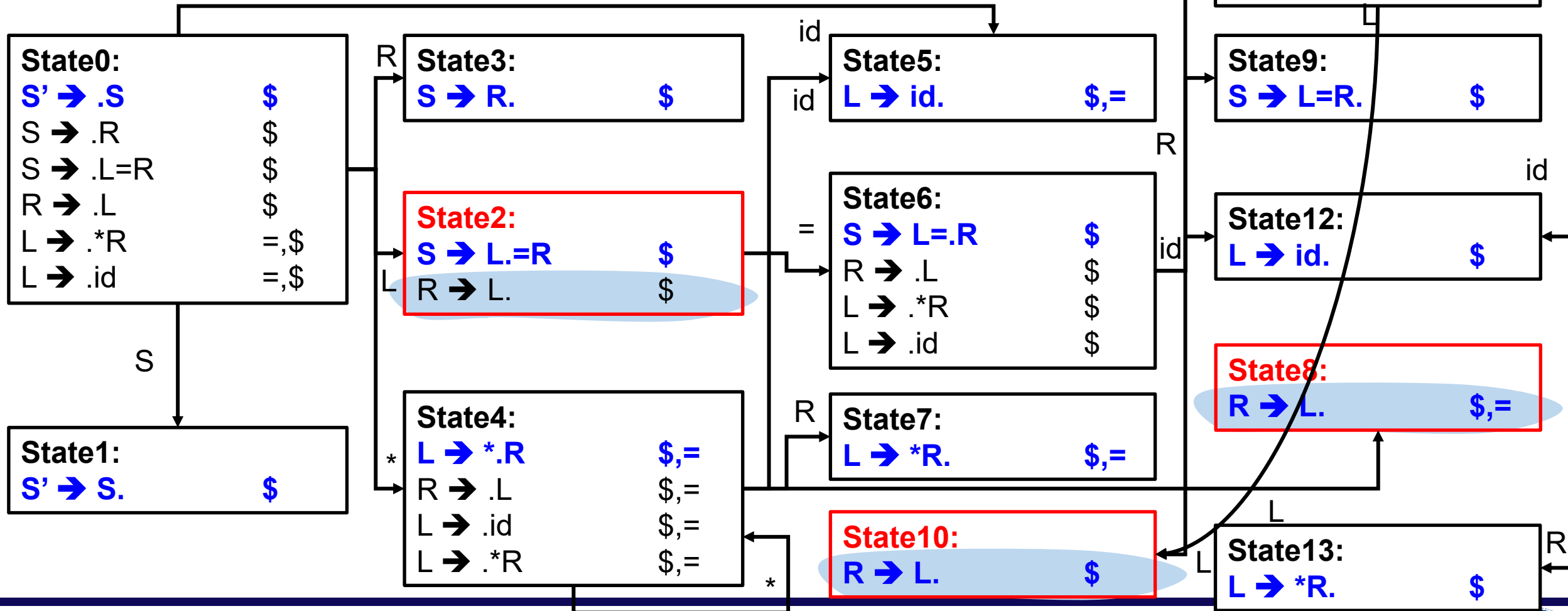
$\text{First}(S) = \{*, \text{id}\}$

$\text{First}(R) = \{*, \text{id}\}$

$\text{First}(L) = \{*, \text{id}\}$

Class Exercise

- LR(1) can differentiate $[S \rightarrow L. = R]$ and $[R \rightarrow L.]$



LALR(1) Parsing

- LR(1) has too many states
- LALR(1) parsing is a lookahead LR
 - Constructs LR(1) DFA and merges any two LR(1) states whose items have the same production rule, but different lookahead
 - Reduces the number of parser table entries
 - Theoretically less powerful than LR(1)

$S \rightarrow id.$	$+$
$S \rightarrow E.$	$\$$

 $+$

$S \rightarrow id.$	$\$$
$S \rightarrow E.$	$+$

 $=$

$S \rightarrow id.$	$\$, +$
$S \rightarrow E.$	$\$, +$

LALR(1) Parsing

- **LALR(1) generally has the same number of states as SLR (much less than LR(1))**
 - For Pascal programming language:
 - SLR requires several hundred states
 - LR(1) requires several thousand states
- **LALR(1) has the same lookahead capability of LR(1) and much better than SLR**

We will not dive into the details of LALR(1)

LL/LR Grammars - 1

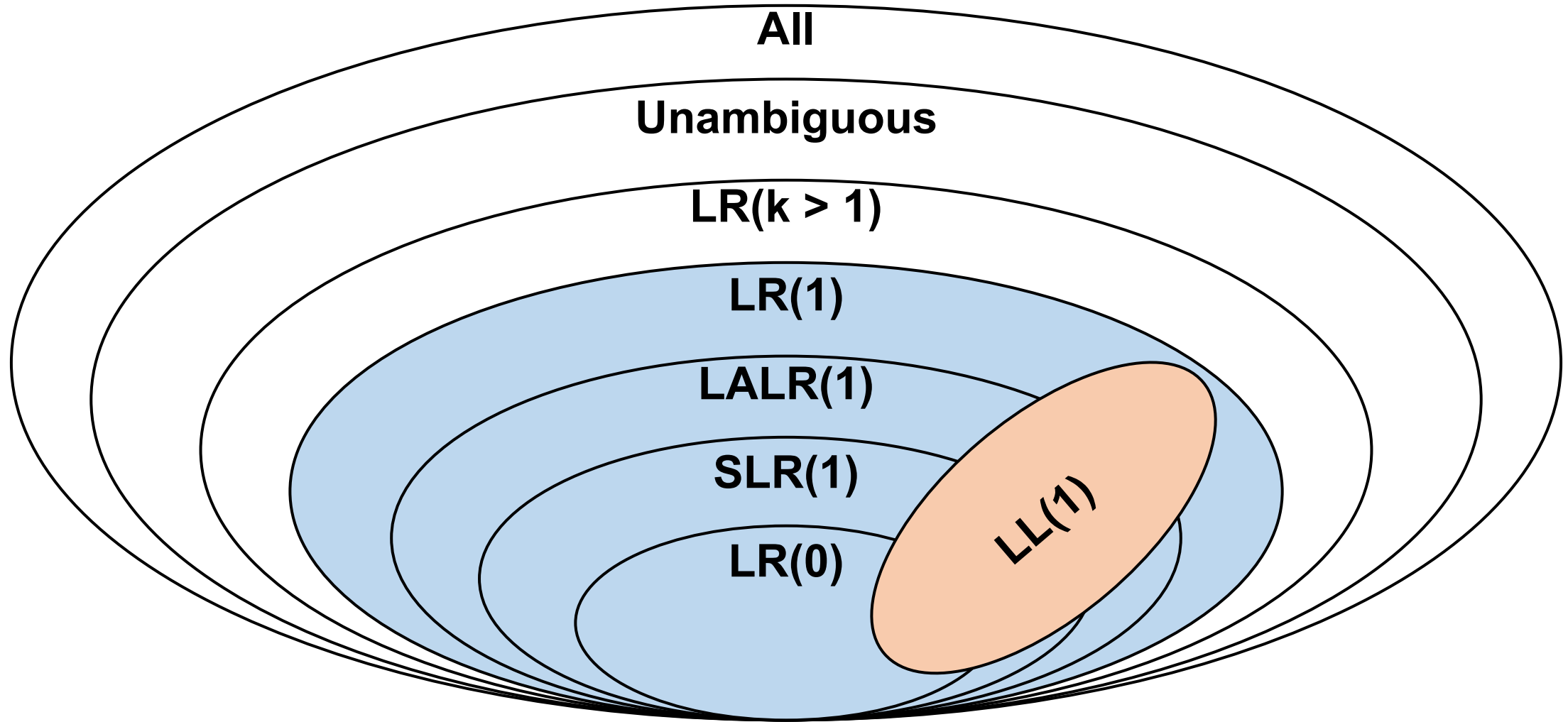
- **LL parsing tables**

- Table[non-terminal, terminal] = Production to apply
- Compute using First and Follow

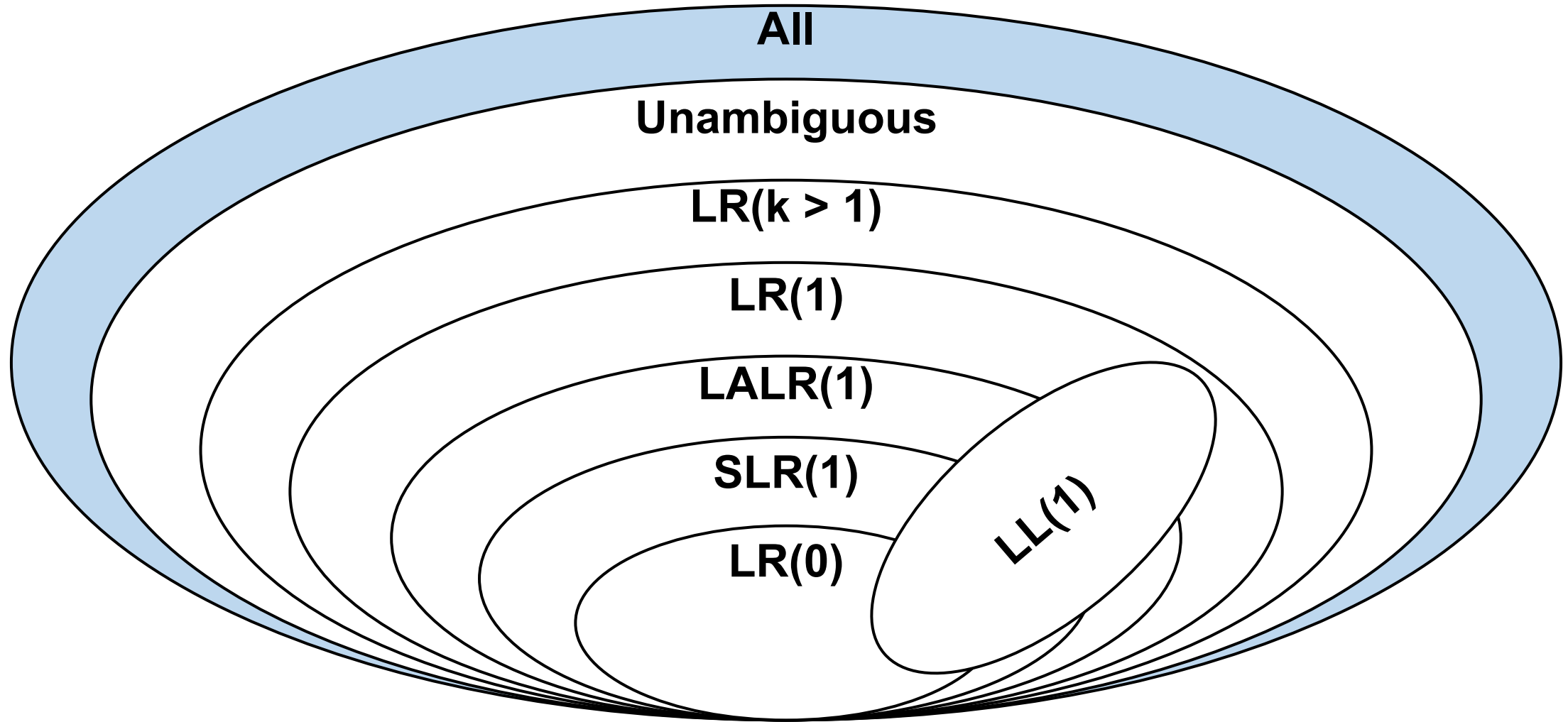
- **LR parsing tables**

- Table[LR state, terminal] = {shift / reduce / error / accept}
- Table[LR state, non-terminal] = {goto / error}
- Compute using closure & goto operations on LR states

LL/LR Grammars - 2



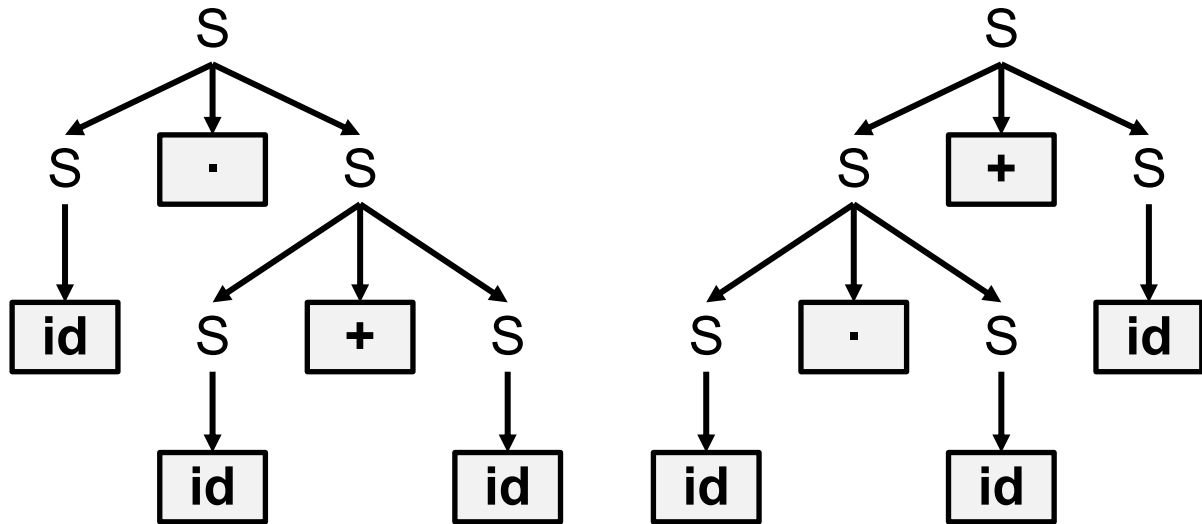
Ambiguous Grammar



Recall: Removing Ambiguity - 1

- **Precedence:**

- The production at higher levels (closer to the root) will have operators with lower priorities (and vice versa)
- We can insert non-terminals to enforce precedence



$S \rightarrow S + S$
 $| S \cdot S | id$

Ambiguous



$S \rightarrow S + T | T$
 $T \rightarrow T \cdot id | id$

Unambiguous

Recall: Removing Ambiguity - 2

- **Associativity:**

- We should determine where to place recursion depending on the associativity
 - Left associative: place the recursion on the left
 - Right associative: place the recursion on the right
 - Non associative: do not use recursion

$$\begin{array}{l} S \rightarrow S - T \mid T \\ T \rightarrow \text{id} \end{array}$$

Left

$$\begin{array}{l} S \rightarrow T \wedge S \mid T \\ T \rightarrow \text{id} \end{array}$$

Right

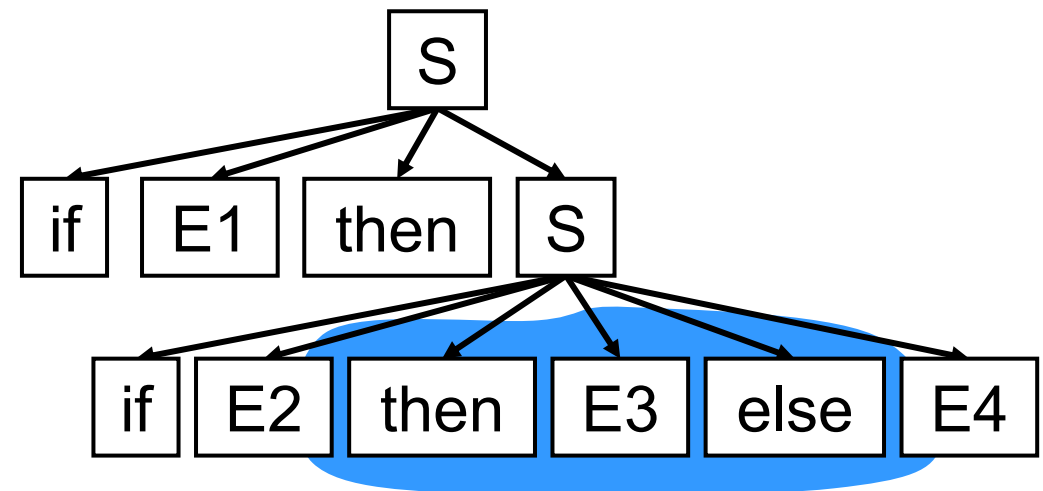
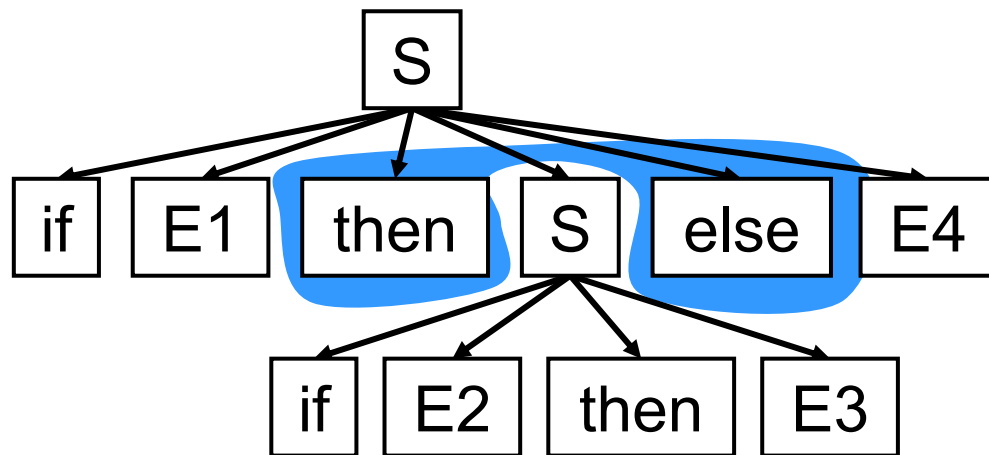
$$\begin{array}{l} S \rightarrow A < A \mid A \\ A \rightarrow \text{id} \end{array}$$

Non

Recall: Removing Ambiguity - 3

- **If/Then/Else**

- We need to find the correct closure if there are both if/then/else and if/then
- Consider “if E1 then if E2 then E3 else E4”
 - $S \rightarrow \text{if } E \text{ then } S \mid \text{if } E \text{ then } S \text{ else } S \mid \text{other}$
 - We should match else to the closest then



Recall: Removing Ambiguity - 4

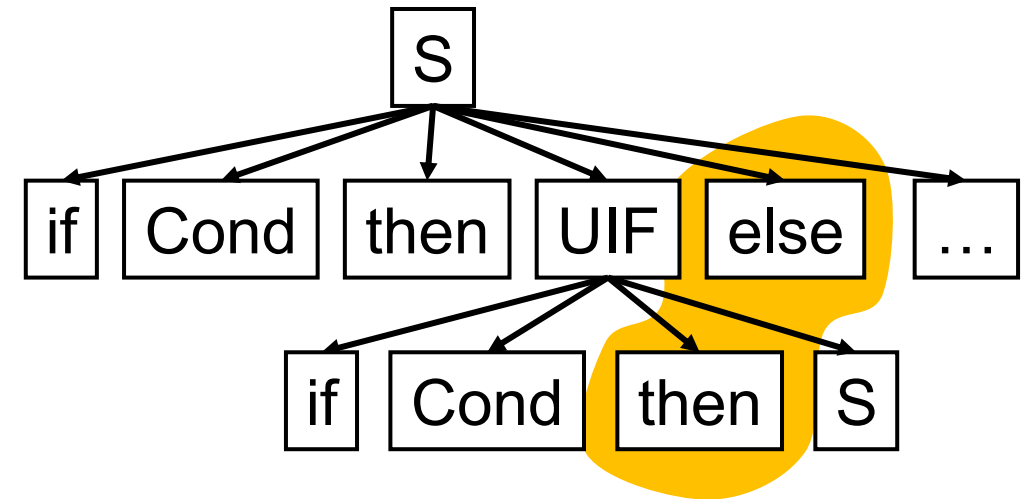
- We should enforce “else” to match the closest then

S → MIF // All “then”s are matched
 | UIF // Some “then”s are unmatched

MIF → if Cond then MIF else MIF
 | Others

UIF → if Cond then S
 | if Cond then MIF else UIF

// Consider if Cond then UIF else S

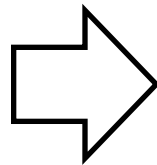


Automatic Disambiguation - 1

- **It is highly complex to propose unambiguous grammars**
 - Precedence: need to consider precedence between different operators
 - Associativity: need to consider associativity of the given operator
- **We can define precedence to use ambiguous grammars w/o shift-reduce conflicts**
 - Define precedence between different types of terminals
 - Define precedence between terminals on the stack vs. terminals on the input

$S \rightarrow S + E \mid E$
$E \rightarrow E * T \mid T$
$T \rightarrow F \mid id$

Unambiguous



$E \rightarrow E + E$
$\mid E * E$
$\mid E \wedge E \mid id$

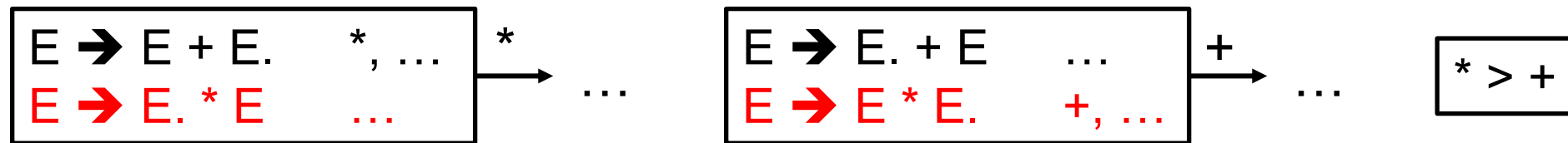
Ambiguous

$Input(\wedge) > Stack(\wedge) >$
$Stack(*) > Input(*) >$
$Stack(+) > Input(+)$

Automatic Disambiguation - 2

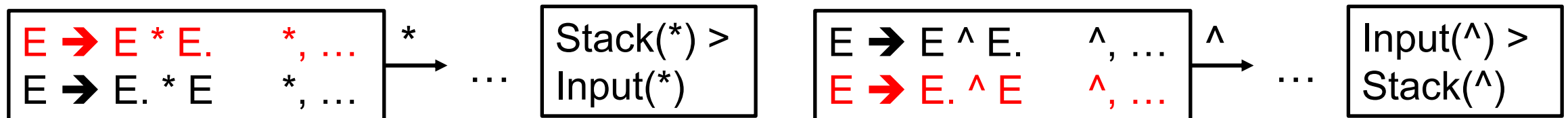
- **Precedence:**

- If precedence of the input token is greater than the last terminal on the stack, favor shift over reduce (vice versa)



- **Associativity**

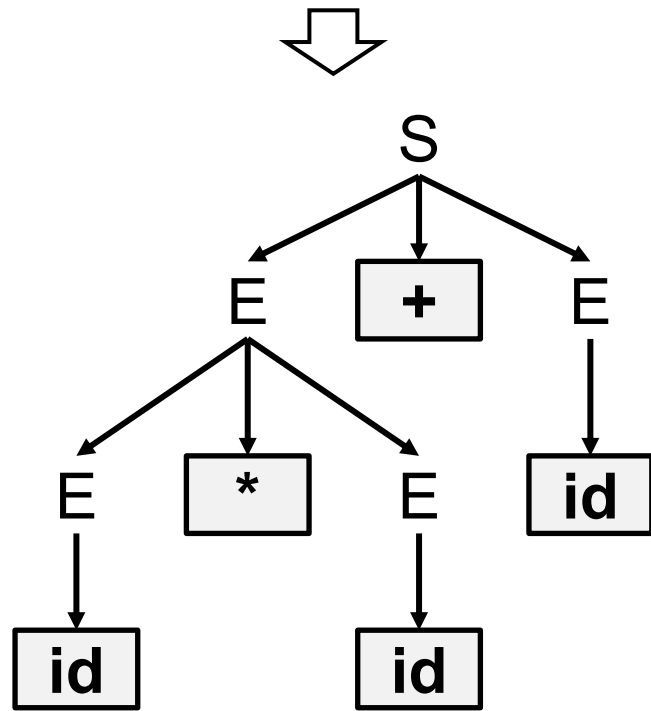
- If an operator is left-associative, assign higher precedence to the operator on the stack (than the one in the input stream)



Recall: AST

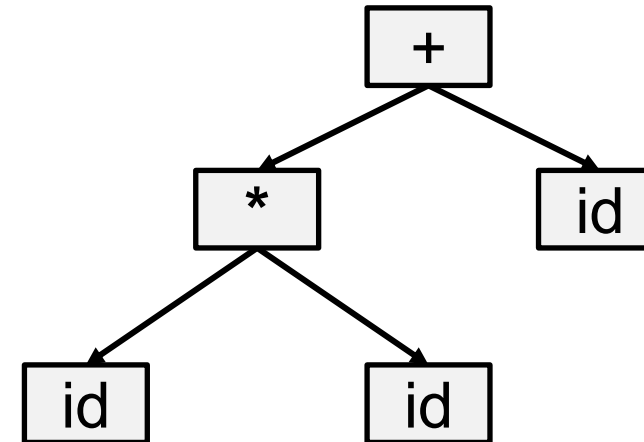
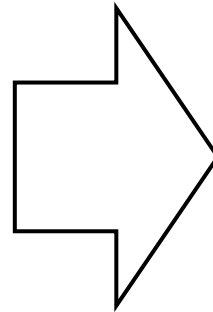
- AST discards unneeded information for syntax analysis

Input = id * id + id



Parse Tree

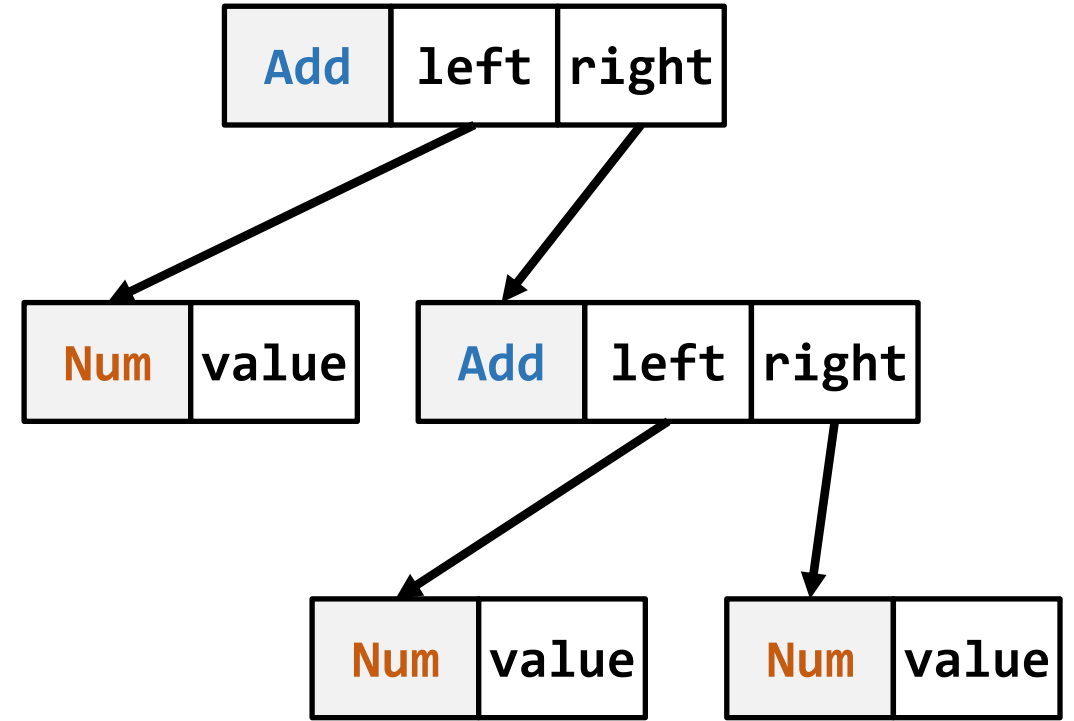
Remove
details



Abstract Syntax Tree

AST Data Structure

```
abstract class expr {}  
  
class Add extends expr {  
    expr left, right;  
    Add (expr L, expr R) {  
        left = L; right = R;  
    }  
}  
  
class Num extends expr {  
    int value;  
    Num (int v) {value = v;}  
}
```



AST Data Structure

Implicit AST Construction

- **LL/LR parsing techniques implicitly build AST**
- **The parse tree is captured in the derivation**
 - LL parsing: AST represented by the productions
 - LR parsing: AST represented by the reductions
- **We should implicitly construct the AST during the parsing phase**

AST Construction: LL

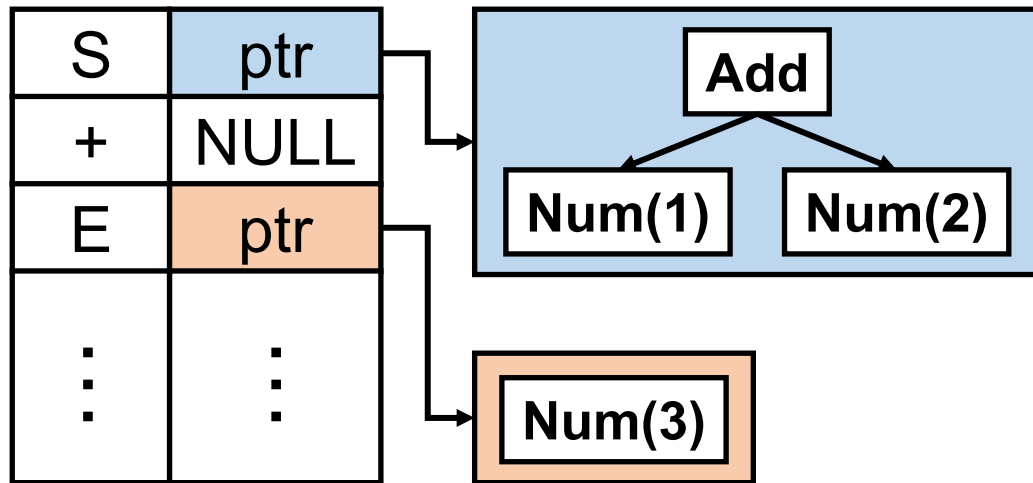
	num	+	(	)	\$ (EOF)
S	ES'		ES'		
S'		+S		ϵ	ϵ
E	num		(S)		

```
expr parse_S() {  
    switch (token) {  
        case num:  
        case '(':  
            expr child1 = parse_E();  
            expr child2 = parse_S'();  
            return new S(child1, child2);  
        default: ParseError();  
    }  
}
```

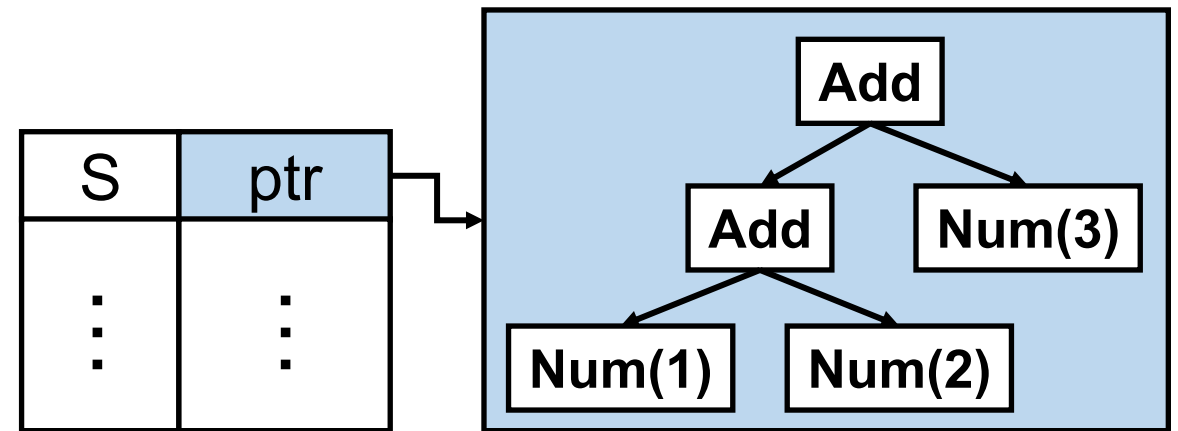
AST Construction: LR

- **AST construction mechanism**

- Store parts of the tree on the stack
- For each nonterminal X on the stack, store the sub-tree for X on the stack
- After reduce operation for a production $X \rightarrow \alpha$, create an AST node for X



Before $S \rightarrow E + S$ Reduction

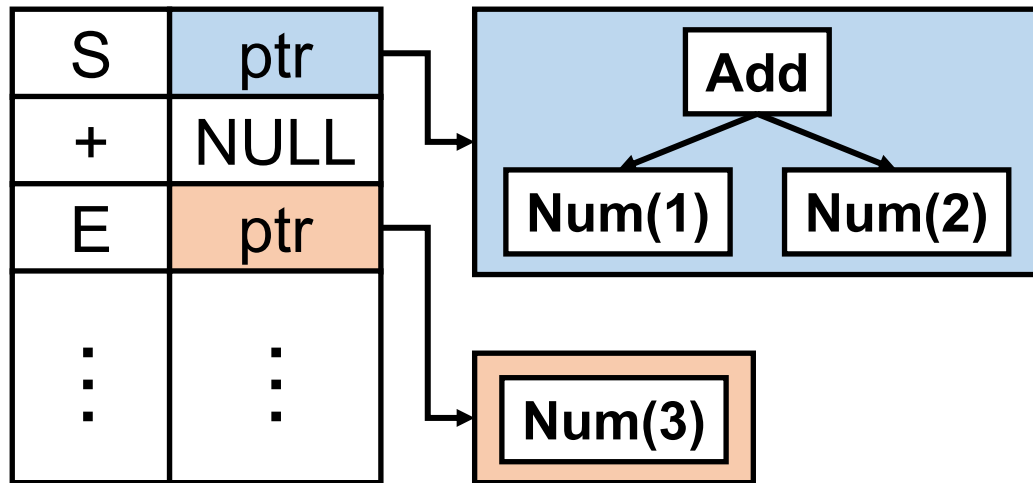


After $S \rightarrow E + S$ Reduction

AST Construction: LR

- **AST construction mechanism**

- Store parts of the tree on the stack
- For each nonterminal X on the stack, store the sub-tree for X on the stack
- After reduce operation for a production $X \rightarrow \alpha$, create an AST node for X



Before $S \rightarrow E + S$ Reduction

```
// For the reduce action
$3 = pop_stack(); // S
$2 = pop_stack(); // +
$1 = pop_stack(); // E
$$ = new S($1, $3);
push_stack($$);
```

After $S \rightarrow E + S$ Reduction

Specification, Recognition, and Automation in Parser

- **Specification:** how to specify valid strings of tokens?
 - Context-free grammars (CFG)
- **Recognition:** how to recognize the specified patterns?
 - Parse tree and abstract syntax tree (AST)
- **Automation:** how to generate parse tree from CFG?
 - Top-down and bottom-up parsing
 - Automatic generation tool (yacc/bison) → Will be covered in the project